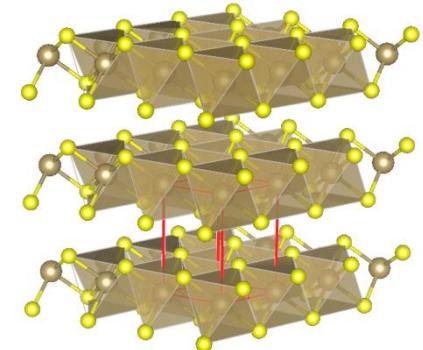
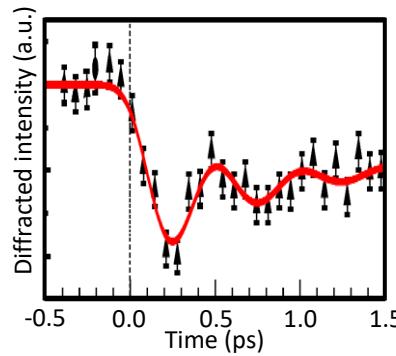
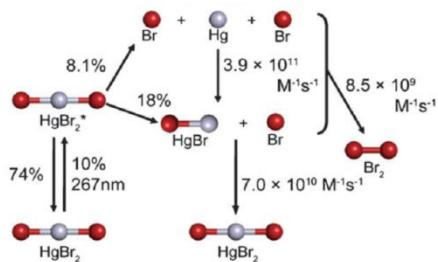
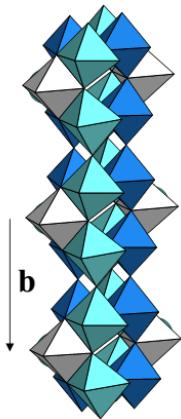


Sub-ns and sub-ps structural dynamics: a view from time-resolved X-ray diffraction



Claire Laulhé



SOLEIL synchrotron - CRISTAL beamline

Paris-Saclay University (Psud)



Sub-ns and sub-ps structural dynamics: a view from time-resolved X-ray diffraction

I. Scientific motivations

II. Pump-probe diffraction

- Principle
- Time resolution & synchronization
- Short X-ray pulse sources
- Specific geometrical constraints

III. Examples

- Photo-induced phase transition in $K_{0.3}MoO_3$
- Ultrafast bond formation in a Gold(I) trimer



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Structural dynamics in physics

- Crystals at thermodynamic equilibrium

Atomic displacements : sum of normal modes

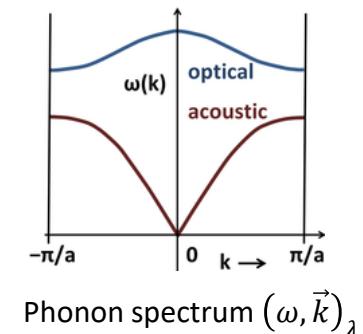
$$\vec{u}_n(\vec{r}, t) = \sum_{\lambda, \|\vec{k}\|} u_n(\lambda, \vec{k}) \vec{e}_{\lambda, \vec{k}} e^{i[\omega(\lambda, \vec{k})t - \vec{k} \cdot \vec{r}]}$$



Longitudinal mode



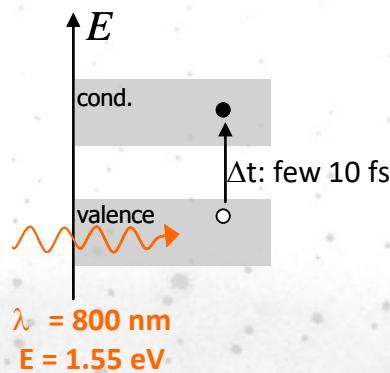
Transverse mode



Phonon spectrum $(\omega, \vec{k})_\lambda$

→ Experiments in the frequency domain: inelastic neutron scattering, Raman scattering...

- Photo-induced structural dynamics



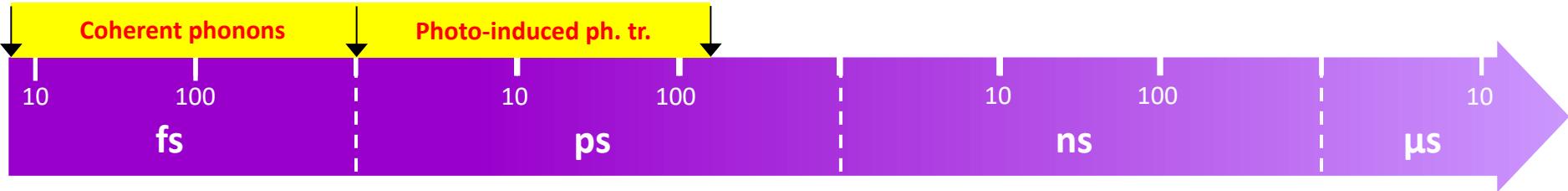
Within few 10 fs: electronic transitions in a « Frozen lattice »

- Decoupled electronic and lattice degrees of freedom
- Out-of-equilibrium dynamics

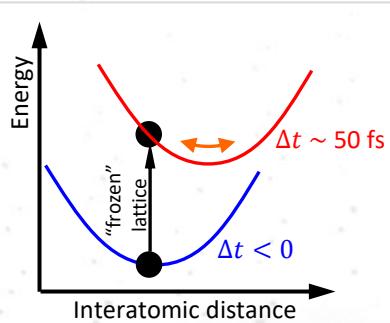
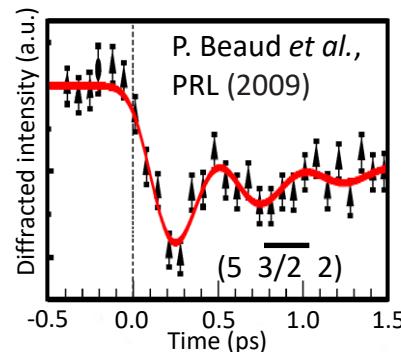
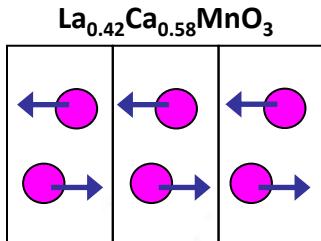
→ Experiments in the time domain: time-resolved pump-probe diffraction



Structural dynamics in physics



$t < \text{few ps}$: coherent phonons

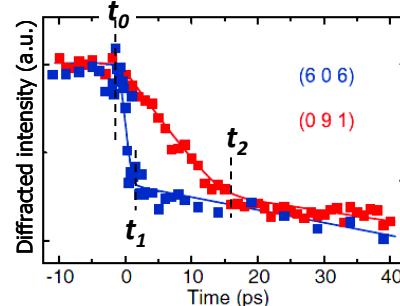
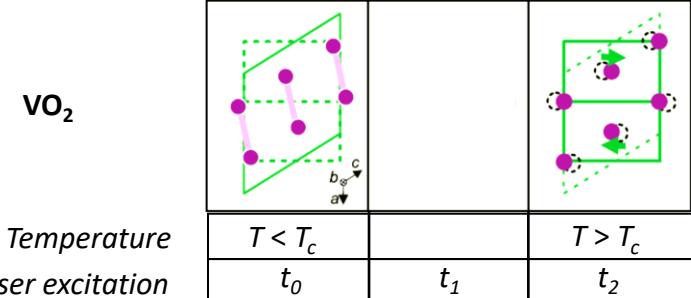


Sudden shift of the quasi-equilibrium atomic positions:

Displacive excitation

H.J. Zeiger *et al.*, PRB **45**, 768 (1992)

$t < \text{few 100 ps}$: ultrafast phase transitions



**Exploration of the potential
in photo-excited states**

**Novel states of matter
Ultrafast control of the physical properties**

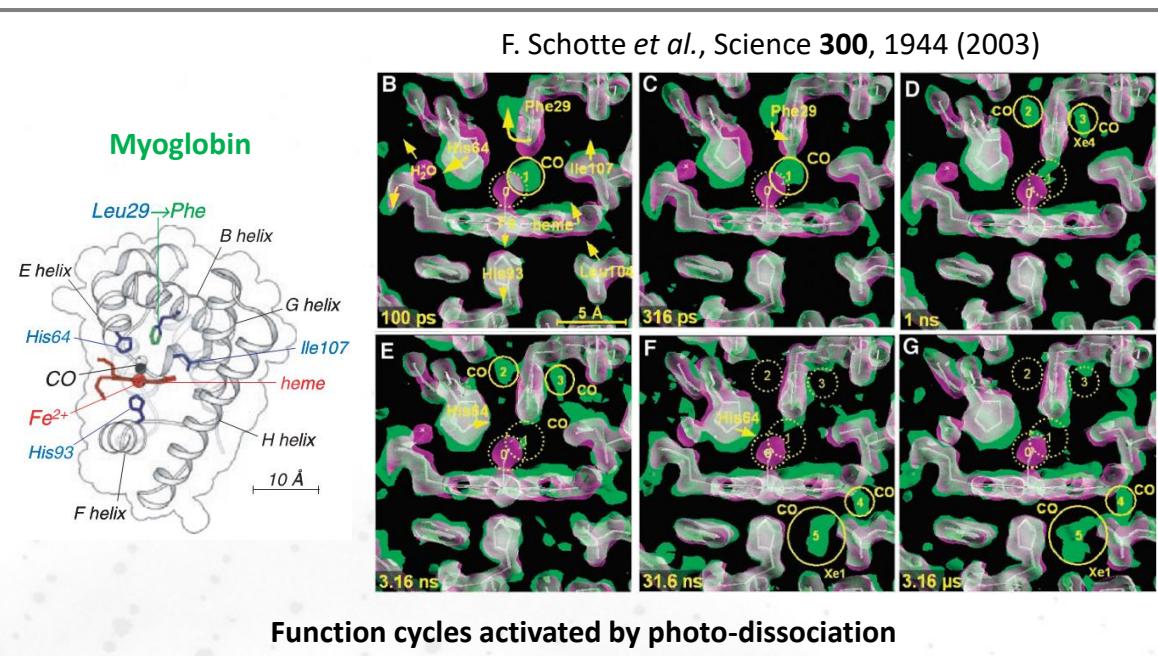
Structural dynamics in biology

- Protein dynamics :

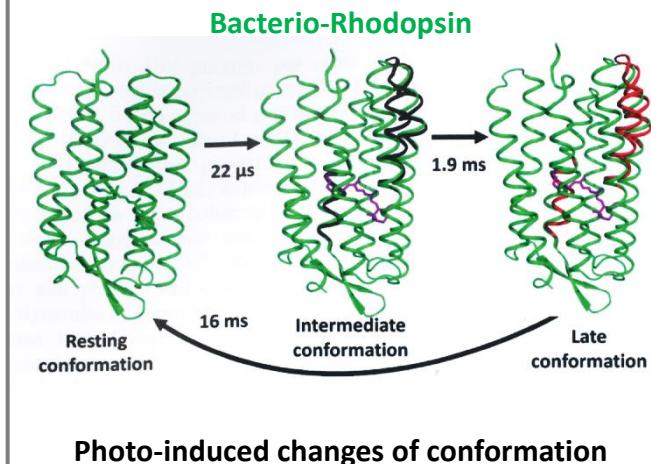
Study of the fastest dynamics:

Reaction mechanisms have to be triggered at the same time within ps !

→ Photo-induced dynamics



M. Andersson et al., Structure 7, 1265 (2009)



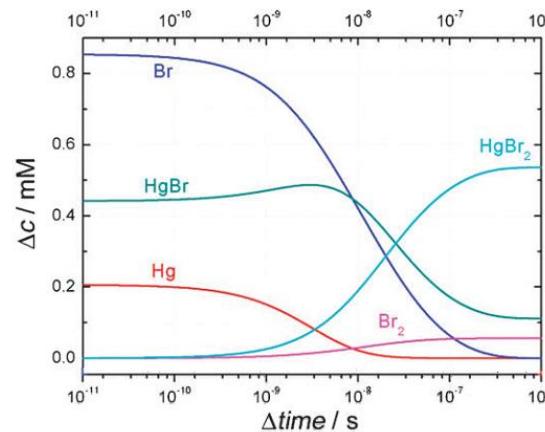
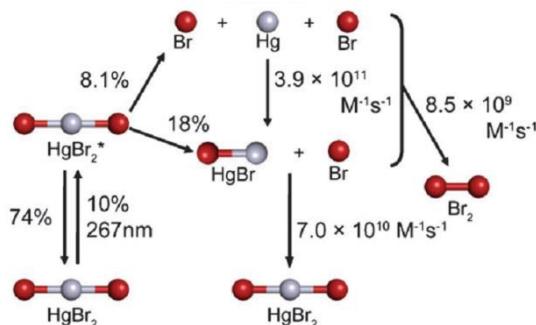
Microscopic understanding of the biological functions



Structural dynamics in chemistry

- Photo-activated chemical reaction processes

Dissociation and recombination of HgBr_2

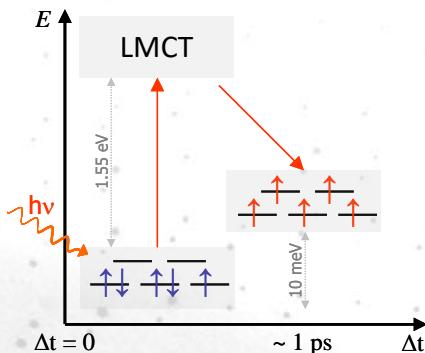
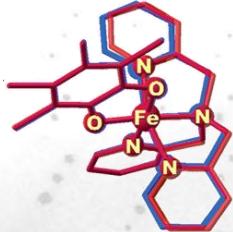


S. Jun *et al.*, Phys. Chem. Chem. Phys. **12**, 11536–11547 (2010)

- Molecular crystals

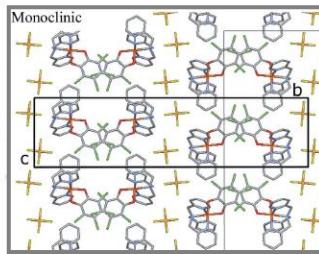
[TPA (FeIII) TCC]

Tris(2-pyridylmethyl)-
3,4,5,6-tetrachlorocatecholate

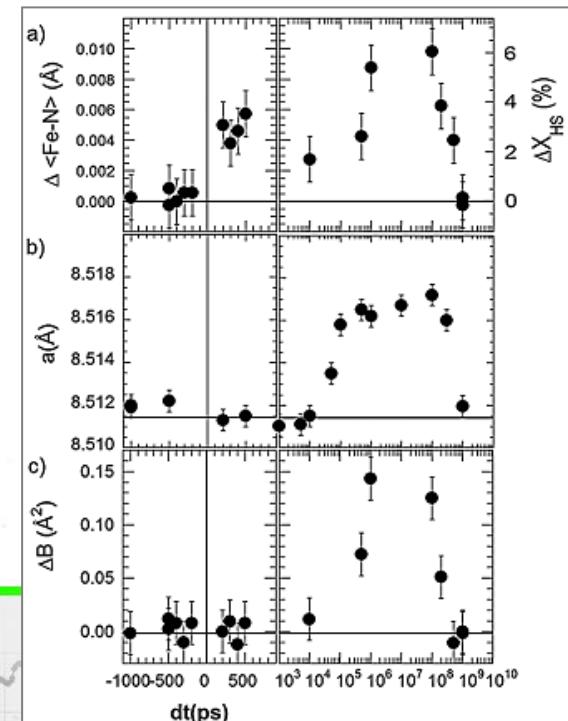


M. Lorenc *et al.*, PRL **103**, 028301 (2009)

[TPA (FeIII) TCC] PF_6^-



Lattice
Cooperative effects!



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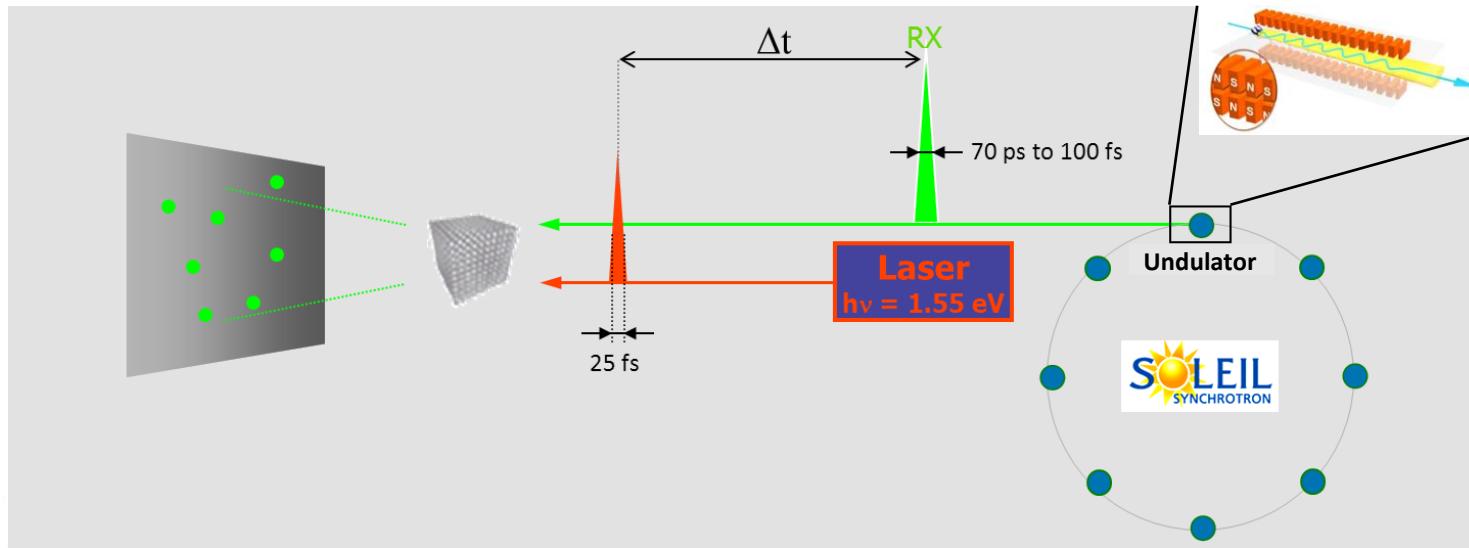
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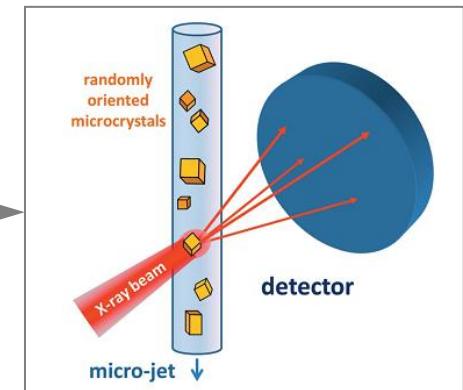


Time-resolved pump-probe diffraction

Following photo-induced structural changes as a function of time



- One pump-probe cycle \leftrightarrow diffraction signal too low !
→ N pump-probe cycles needed for each Δt : study of reversible processes
- Irreversible processes : liquid jets or serial crystallography at X-FELs
- A crucial parameter : control of Δt [quality of synchronization]



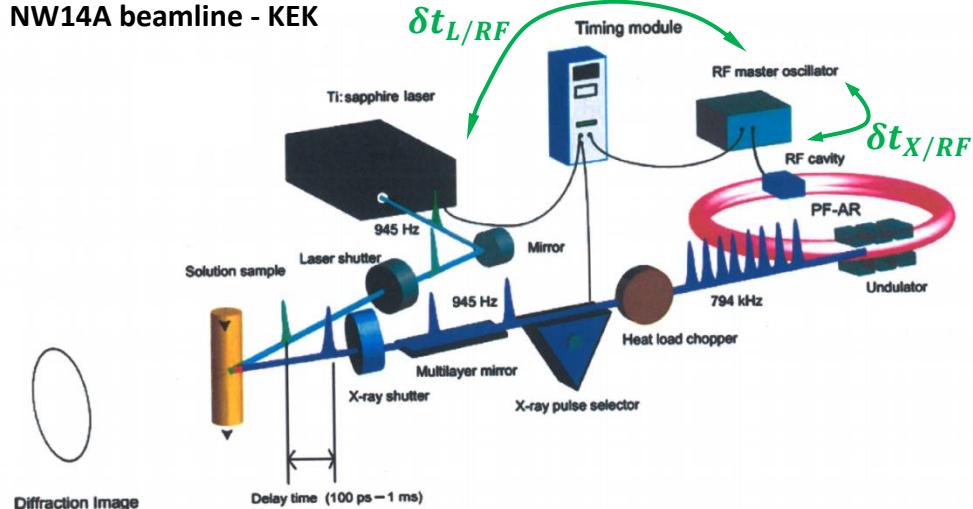
I. Schlichting, IUCrJ **2**, 246–255 (2015)

V. Panneels *et al.*, Structural Dynamics **2**, 041718 (2015)

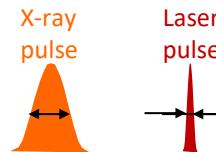
T. R. M. Barends, Science **350**, 445 (2015)

Synchronization scheme

NW14A beamline - KEK



H. Ihee, Int. Rev. Phys. Chem. **29**, 453-520 (2010)



$$\delta t^2 = \delta t_L^2 + \delta t_X^2 + \delta t_{X/RF}^2 + \delta t_{L/RF}^2$$

jitter terms (few ps)

- Atomic vibrations: $E = \hbar\omega \sim 20 \text{ meV} \Rightarrow T_{\text{osc}} \sim 250 \text{ fs}$
→ Need for time resolutions of few 10 fs

- Commercially available Ti:Sa lasers (1990 →): ~ 40 fs pulses @ 800 nm [1.55 eV]



Chirped pulse amplification

G. Mourou, D. Strickland (2018 Nobel Prize in physics)

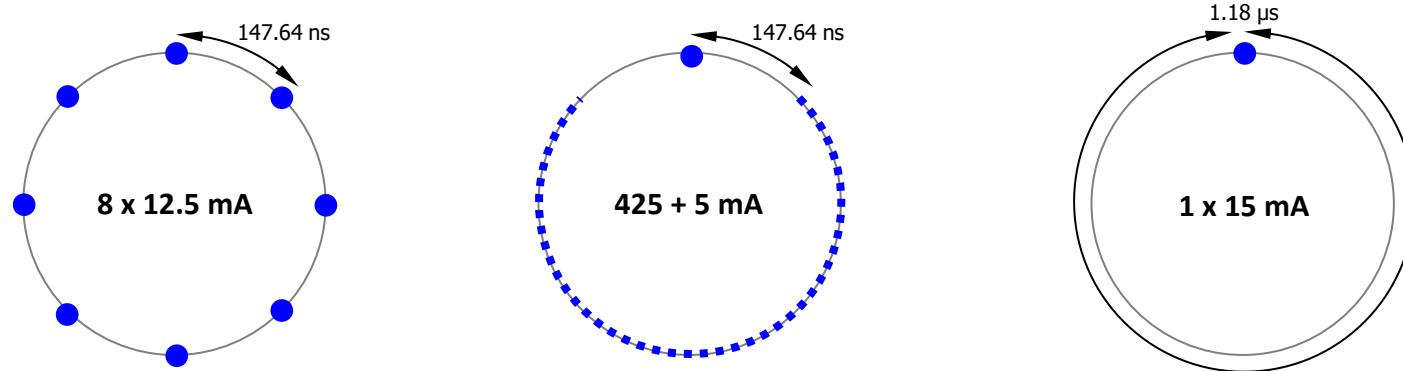
Non-linear optics:

far-infrared (20 μm, 60 meV) ↔ ultraviolet (60 eV, 20 nm)

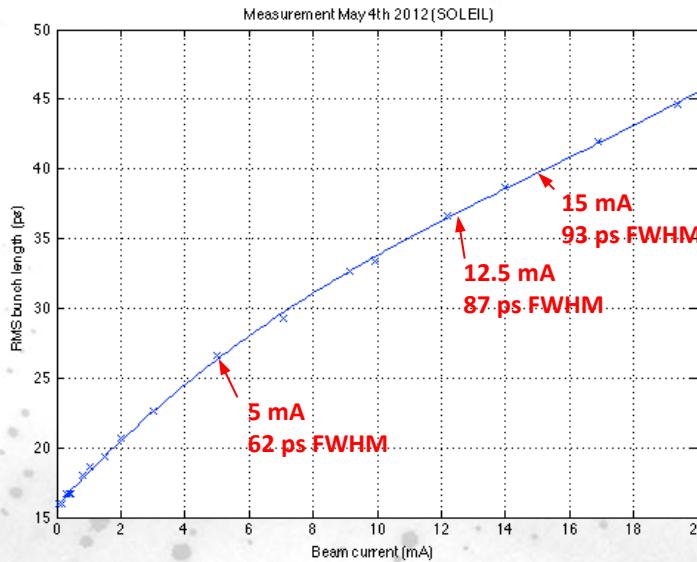


X-ray pulse sources

- Few 10 ps pulses from synchrotrons



Bunch modes for time-resolved experiments at SOLEIL



Modes dedicated to time-resolved experiments:

Isolated bunch with high current

Enables pulse selection

Optimized count rate
from selected pulses



X-ray pulse sources

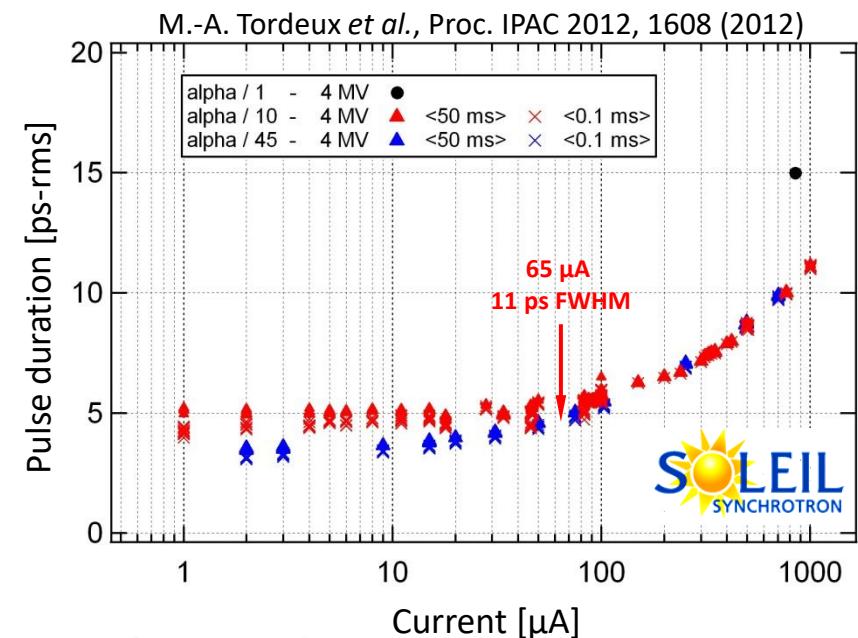
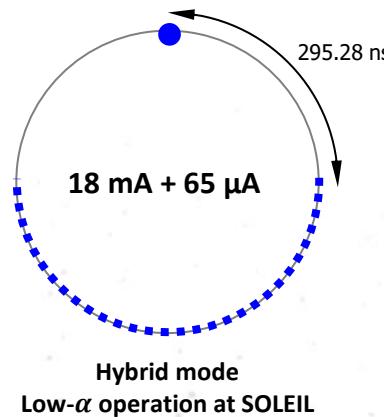
- Few ps pulses from synchrotrons: low- α mode

Normal operation:

- Optics optimized for a low-emittance electron beam
- Dispersion of E_{e^-} \Rightarrow dispersion of e^- revolution period
- Elongated e^- bunches, longer X-ray pulses

Quasi-isochronous ring:

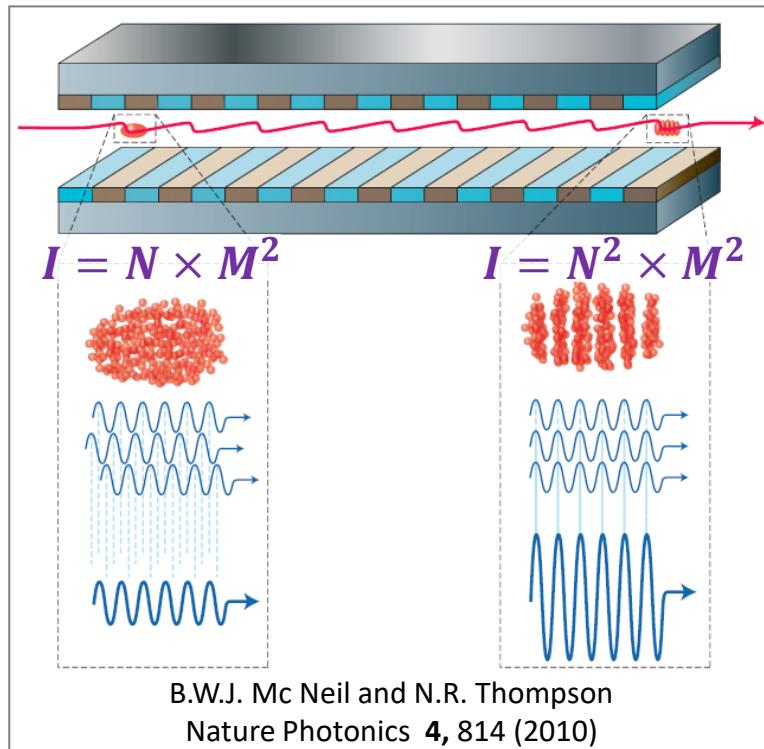
- Electron revolution period independent of ΔE_{e^-}
- Shorter e^- bunches
- Lower bunch currents!



→ User operation at BESSY, SOLEIL, DIAMOND

X-ray pulse sources

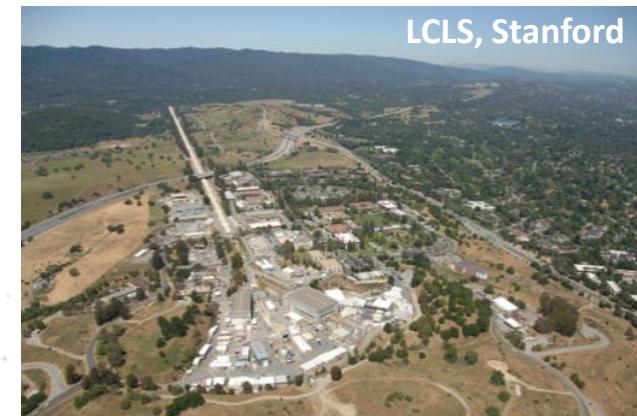
- 100 fs X-ray pulses: X-FELs (2009 →)



**10¹¹ ph./pulse
@100Hz
80 fs duration**

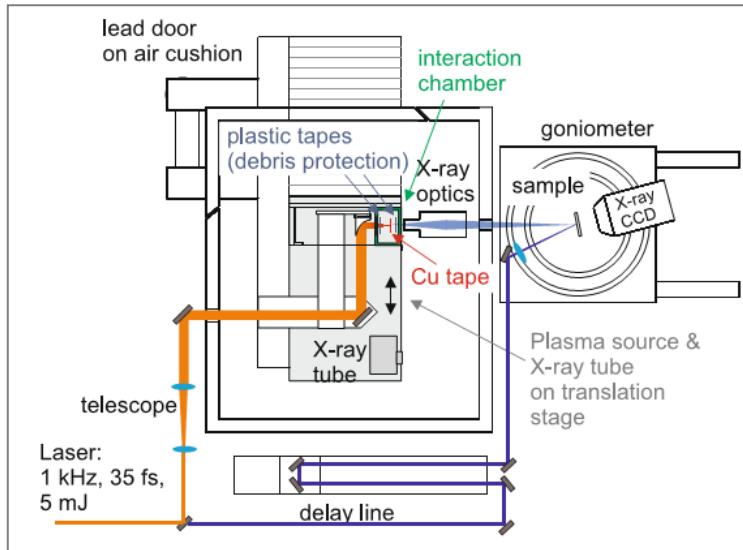
- Short electron pulses produced by a laser-driven electron gun [N electrons]
- Propagation in long undulators (100 m) [M poles]
- Electron beam bunching
→ Coherent emission of all the electrons

**$I \propto N^2 \times M^2$: very high flux
80 fs hard X-ray pulses**



Time-resolved pump-probe diffraction: laser-based sources

- X-ray plasma sources (1994 →)

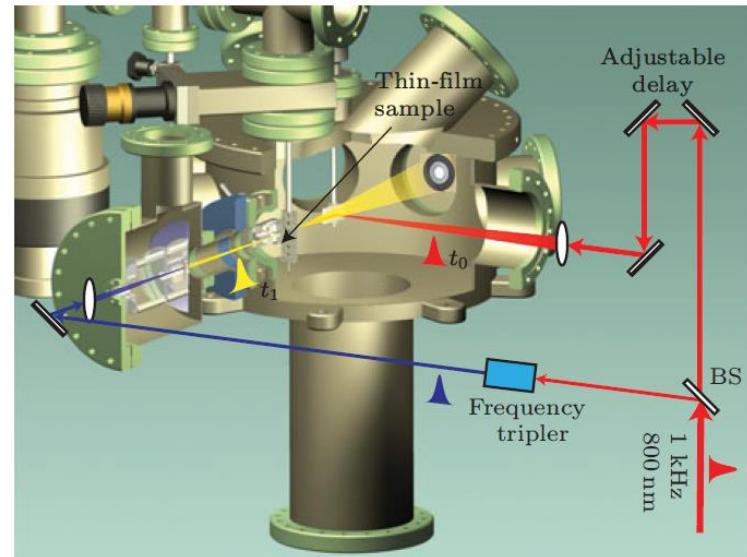


- Laser pulse onto a copper target
- Indirect ionization of Cu atoms
- Emission of X-rays with $K_{\alpha}(Cu)$ wavelength [$\lambda = 1.54 \text{ \AA}$]

**10³ ph./pulse
@1kHz
100 fs duration**

F. Zamponi, Appl. Phys. A **96**, 51-58 (2009)
A. Rousse *et al.*, PRE **50**, 2200 (1994)
A. Rousse *et al.*, Nature **410**, **65** (2001)

- Ultrafast electron diffraction (2003 →)



- Frequency-tripled Ti:Sa laser pulse ($\lambda = 266 \text{ nm}$)
- Pulse-driven photocathode → photoemission
- Acceleration to $\sim 60 \text{ keV}$ [$\lambda \sim 0.05 \text{ \AA}$]

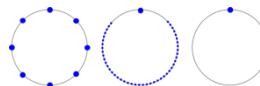
**10³ e⁻/pulse
@1kHz
300 fs duration**

W.-X. Liang *et al.*, Chinese Phys. Lett. **26**, 020701 (2009)
R. Srinivasan *et al.*, Helvetica Chimica Acta **86**, 1761-1799 (2003)

Pump-probe diffraction : typical photon or electron fluxes

Synchrotrons [repetition rate 1 kHz]

- 80 ps X-ray pulses



10⁶ photons/pulse
 $\Delta E/E \sim 10^{-4}$

10⁹ ph/s

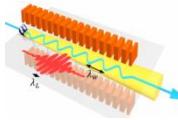
- Few ps X-ray pulses (low- α)



10⁴ photons/pulse
 $\Delta E/E \sim 10^{-3}$

10⁷ ph/s

- 100 fs X-ray pulses (femto-slicing)



10³ photons/pulse
 $\Delta E/E \sim 8.10^{-3}$

10⁶ ph/s

Laser-based sources [repetition rate 1 kHz]

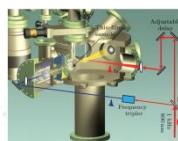
- 100 fs X-ray pulses (plasma source)



10³ photons/pulse
 $\Delta E/E \sim 10^{-4}$

10⁶ ph/s

- 300 fs electron pulses



10³ electrons/pulse

10⁶ e⁻/s

X-ray free electron lasers [repetition rate 100 Hz]

- 80 fs X-ray pulses



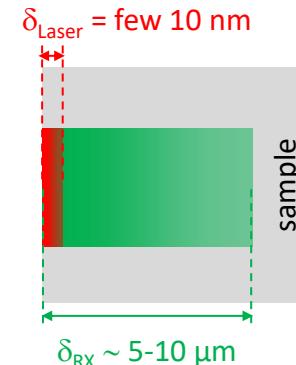
10¹¹ photons/pulse
 $\Delta E/E \sim 10^{-3}$

10¹³ ph/s



Time resolved X-ray diffraction: experimental facts

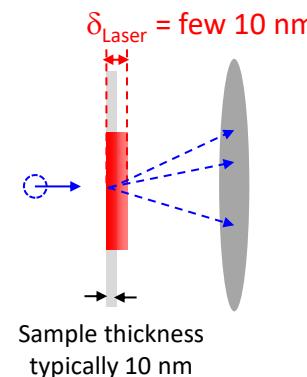
- X-rays and IR photons: differing penetration depths !



!! $v_{\text{probed}} > v_{\text{pumped}}$!!

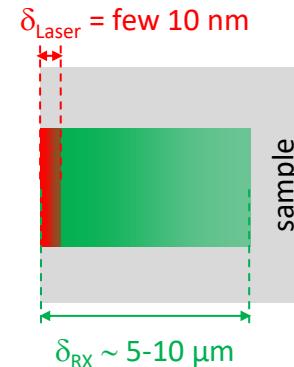
[Typical values for hard condensed matter, 7 keV X-ray photons]

- Electron diffraction: sample is usually thinner than δ_{Laser}



Time resolved X-ray diffraction: experimental facts

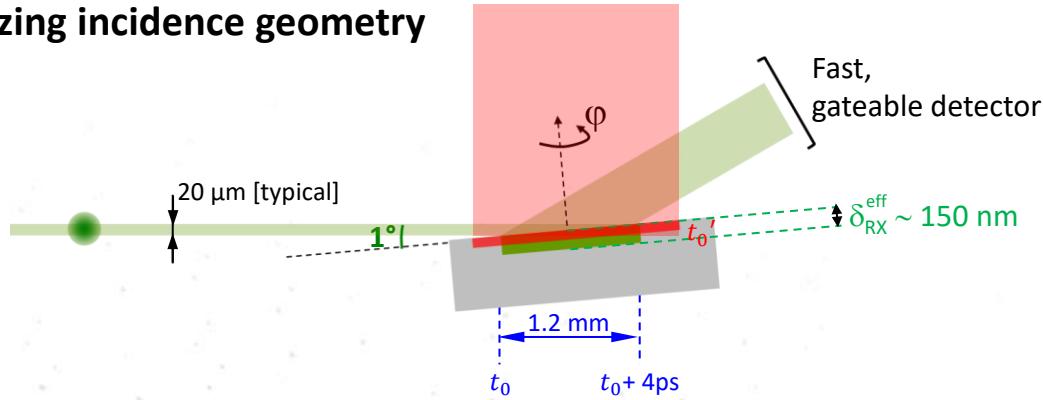
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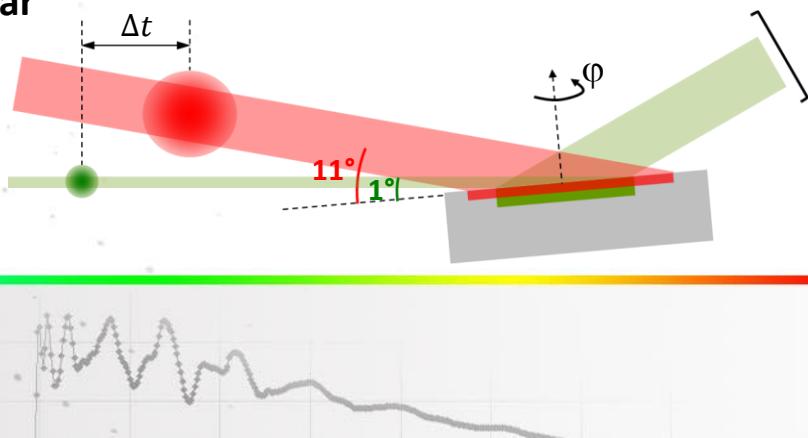
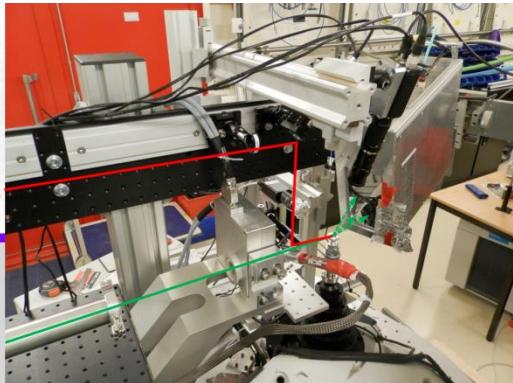
[Typical values for hard condensed matter, 7 keV X-ray photons]

- Grazing incidence geometry

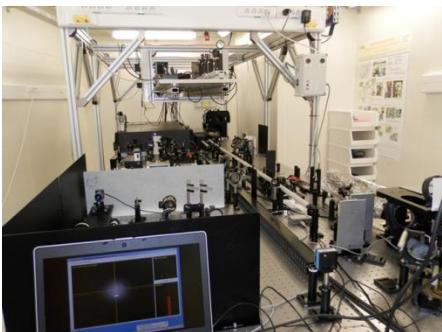


!! Loss of effective time resolution from the difference in relative arrival times between the pump and X-ray beams !!

- Grazing incidence geometry, pump & probe beams collinear

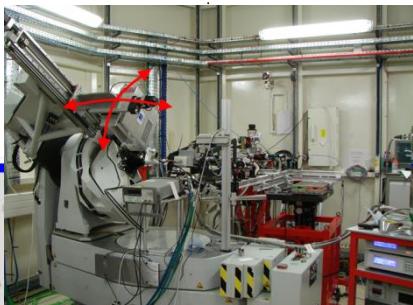
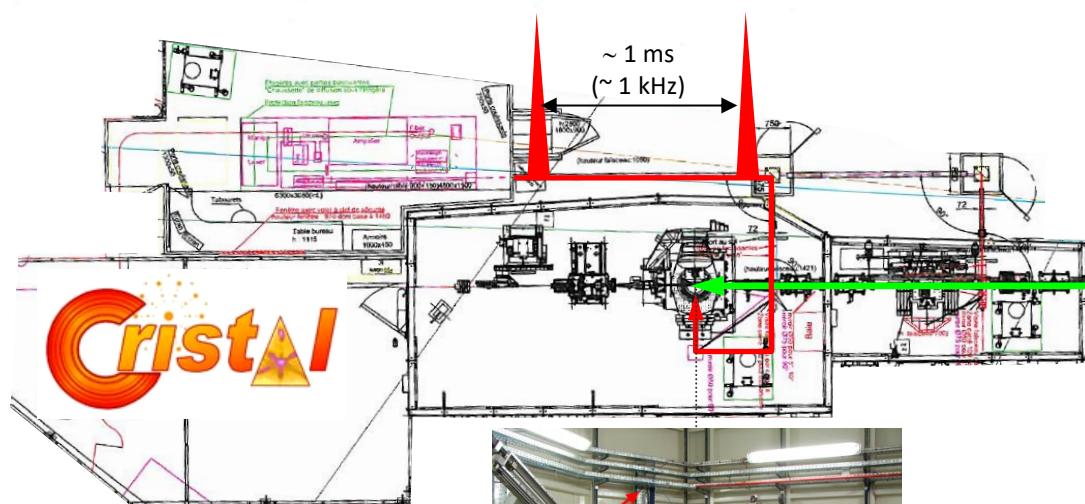
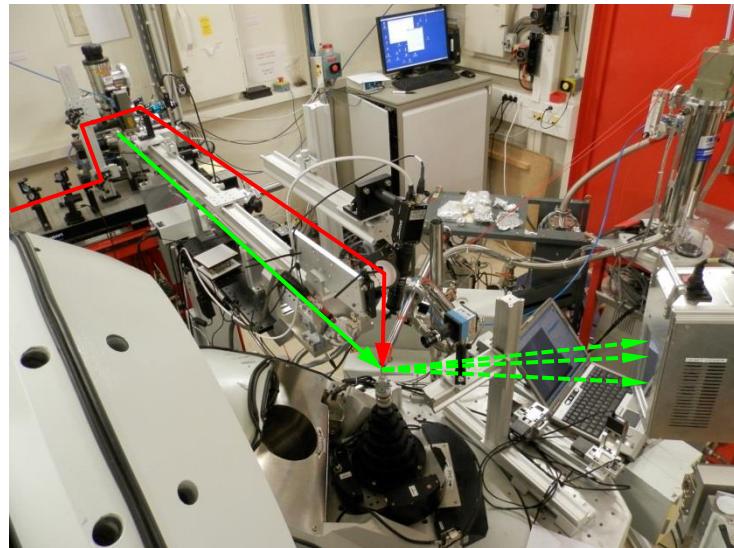


Time-resolved diffraction setup installed at CRISTAL (SOLEIL synchr.)

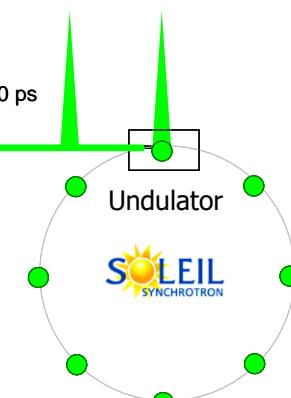


Ti:Sa oscillator + amplifier

$\lambda = 800 \text{ nm}$, 40 fs FWHM
500 $\mu\text{J}/\text{pulse}$ @10kHz, 5 mJ/pulse @1kHz



- X-ray optics:**
- Monochromator
 - Si(111) [2.4 10^{-4} bwth]
 - ML [8.0 10^{-3} bwth]
 - Vertically focusing mirrors



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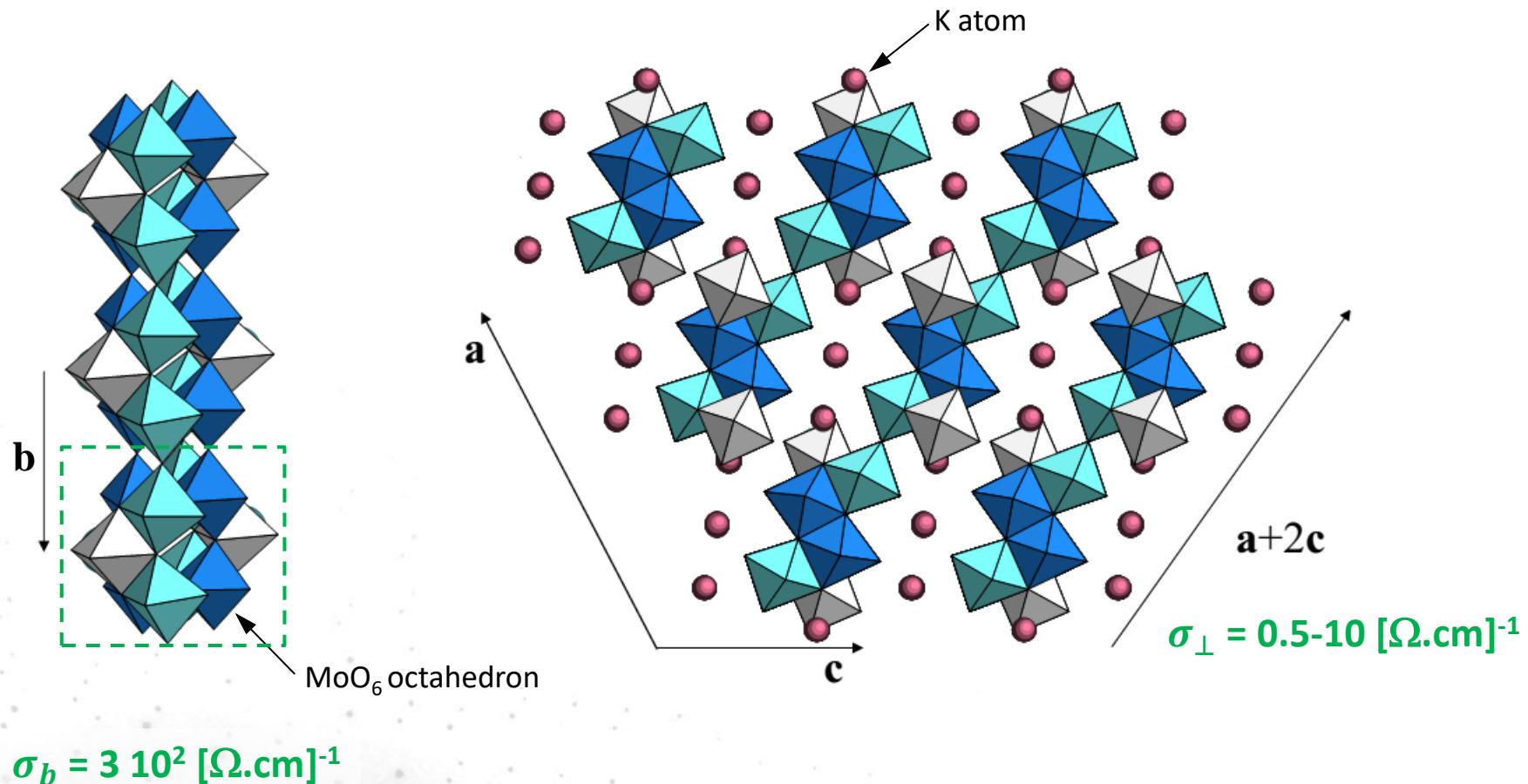
III. Examples

- Photo-induced phase transition in $K_{0.3}MoO_3$
- Ultrafast bond formation in a Gold(I) trimer



Atomic structure of blue bronze ($K_{0.3}MoO_3$)

- A quasi-one-dimensional conductor...



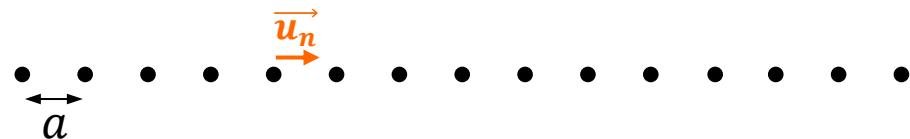
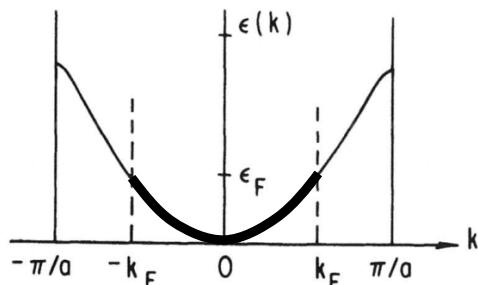
...which undergoes a transition to a charge density wave phase at 183 K

J. Graham and A.D. Wadsley, Acta Cryst. **20**, 93 (1966)
G. Grüner, "Density waves in solids"

Formation of a charge density wave - Peierls model

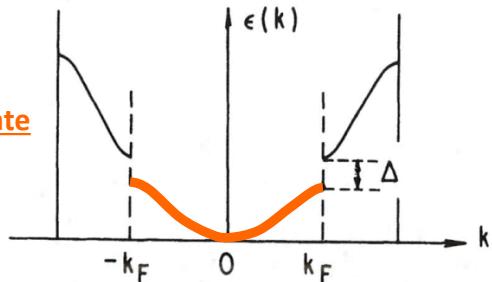
- A metal-insulator transition driven by a periodic lattice distortion

Metallic state

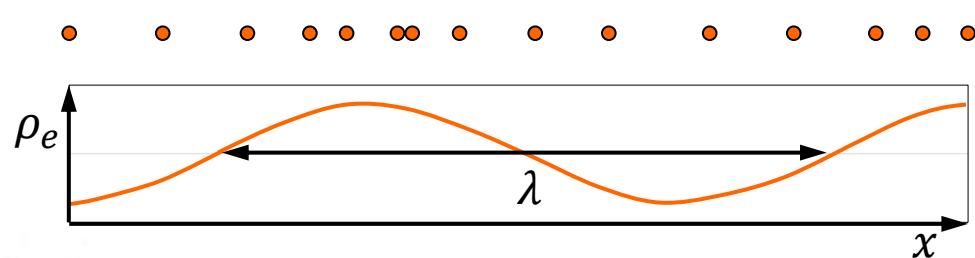


$$\vec{u}_n = \vec{u}_0 \sin(\vec{k} \cdot \vec{R}_n + \varphi) \quad \vec{k} = 2\vec{k}_F, \quad \lambda = \frac{2\pi}{k} = \frac{\pi}{k_F}$$

Charge density wave state
(CDW)



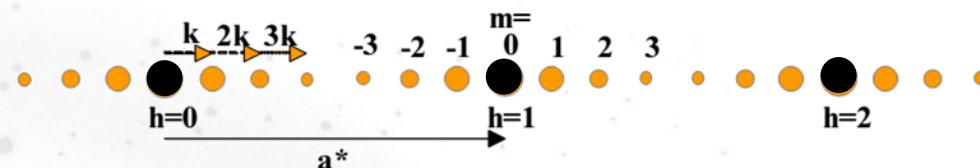
Gain in electronic energy



...At the expense of a moderate cost in elastic energy

CDW systems: strong e-ph coupling

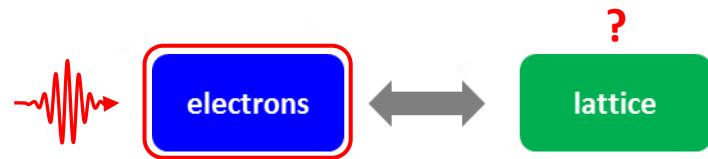
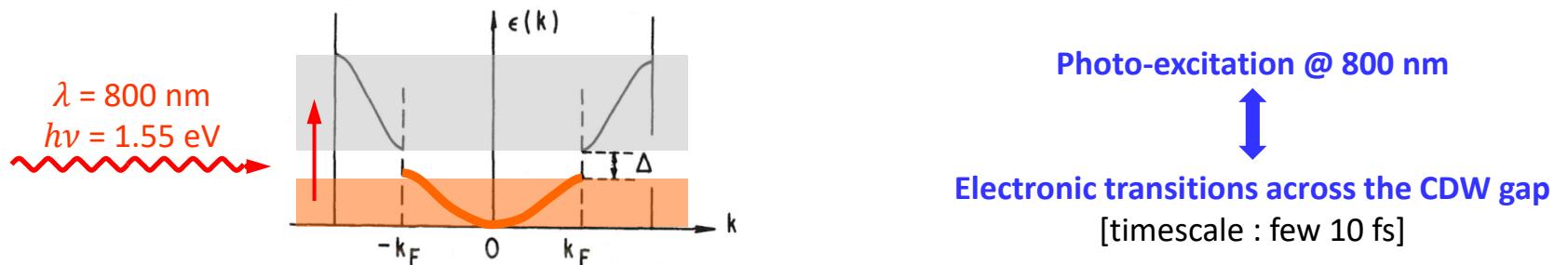
- Diffraction pattern: satellite peaks



$$I_{sat} \propto \|\vec{u}_0\|^2$$



Ultrafast light control of the physical properties of CDW compounds ?

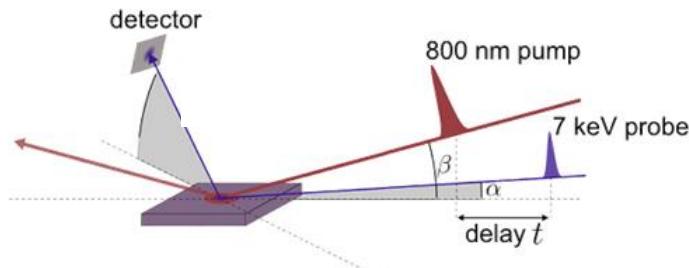


e-ph coupling...
Does photo-excitation affect the CDW structural modulation ?
On which timescale ?

- Photo-induced phase transitions: an out-of-equilibrium dynamical process
 - Control of physical properties on ultrafast timescales (< 1 ps)
 - Discovery of new, intermediate states



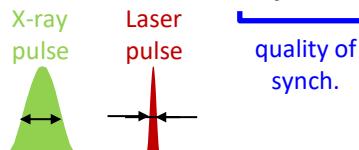
Ultrafast light control of the physical properties of CDW compounds ?



Pump-probe diffraction

Photo-induced structural dynamics in CDW compounds

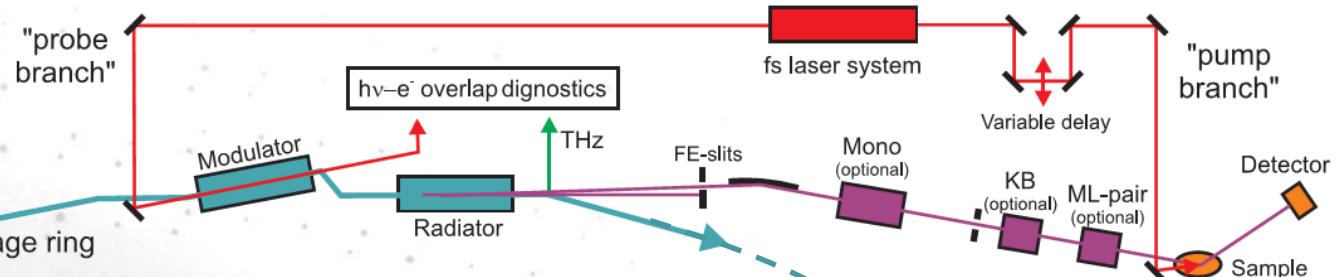
$$\delta t^2 = \delta t_X^2 + \delta t_L^2 + \delta t_{jitter}^2$$



Time resolution needed: down to 100 fs

$$[E_{ph} = \hbar\omega \sim 20 \text{ meV} \Rightarrow T_{osc} \sim 250 \text{ fs}]$$

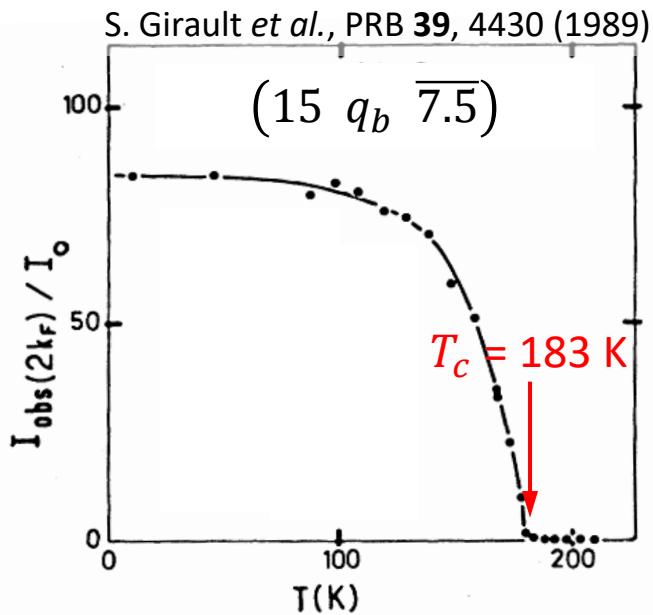
- Use of the synchrotron femto-slicing source at Swiss Light Source



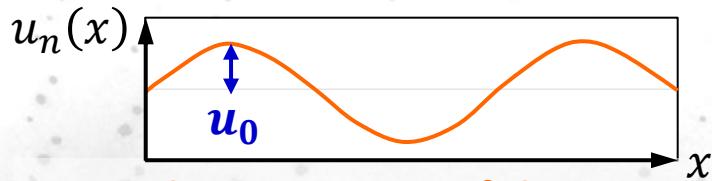
P. Beaud et al., PRL 99 174801 (2007)

Appearance of a charge density wave in blue bronze ($K_{0.3}MoO_3$)

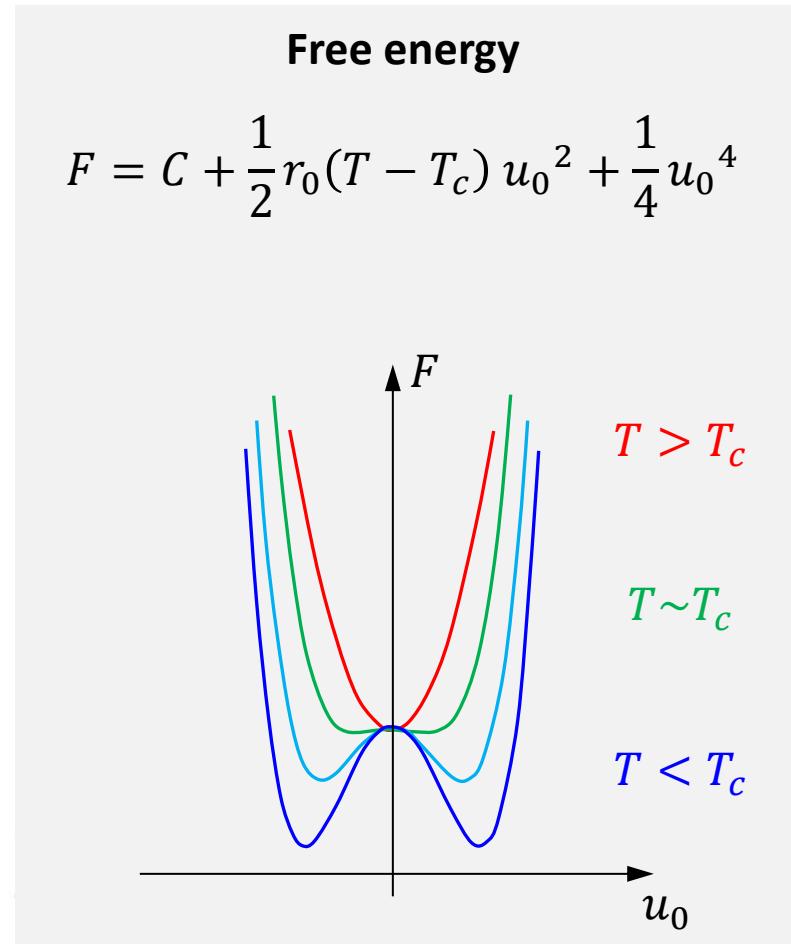
- $K_{0.3}MoO_3$: satellite peaks @ $(h \ k \ l) + (1 \ q_b \frac{1}{2})$



$$I_{\text{sat}} \propto \|\vec{u}_0\|^2$$

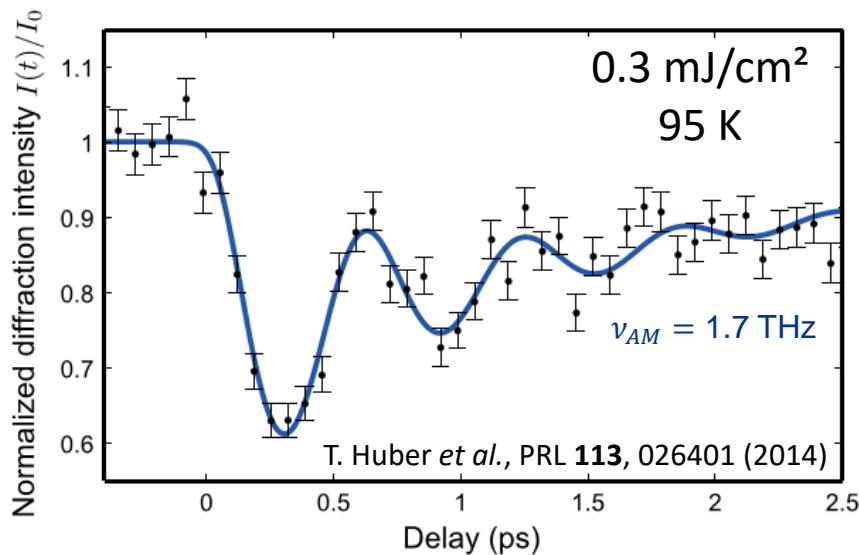


u_0 : order parameter of the transition



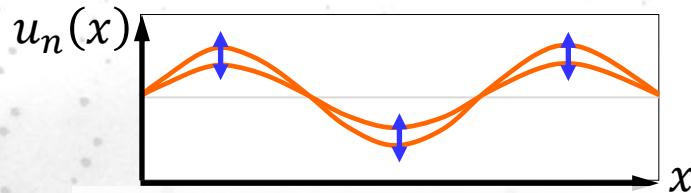
Coherent structural dynamics in blue bronze ($K_{0.3}MoO_3$)

- Time-dependence of the satellite $\left(1 [4 - q_b] \frac{1}{2}\right)$ - Low fluence



$$I_{sat} \propto \|\vec{u}_0\|^2$$

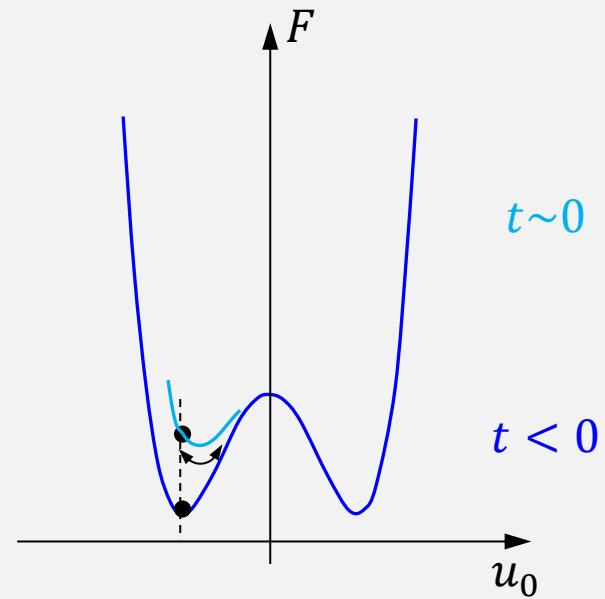
Oscillations of the order parameter u_0 in time



Amplitude mode (AM) of the CDW

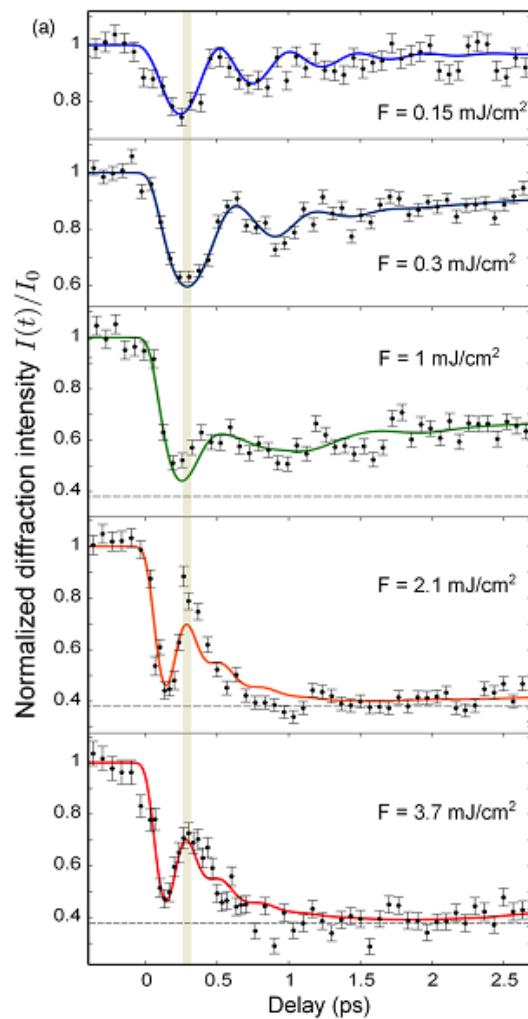
Displacive excitation of the AM:

$$\frac{u_0(t)}{u_0(t < 0)} = A_{disp} [\cos 2\pi\nu_{AM}(t) e^{-t/\tau_{AM}} - e^{-(t)/\tau_{disp}}]$$



Coherent structural dynamics in blue bronze ($K_{0.3}MoO_3$)

- Time-dependence of the satellite $\left(1 [4 - q_b] \frac{1}{2}\right)$ - Higher fluences



- $F = 1 \text{ mJ/cm}^2$

- The recovery time of satellite peak intensity increases
- Coherent oscillations: hardly observable

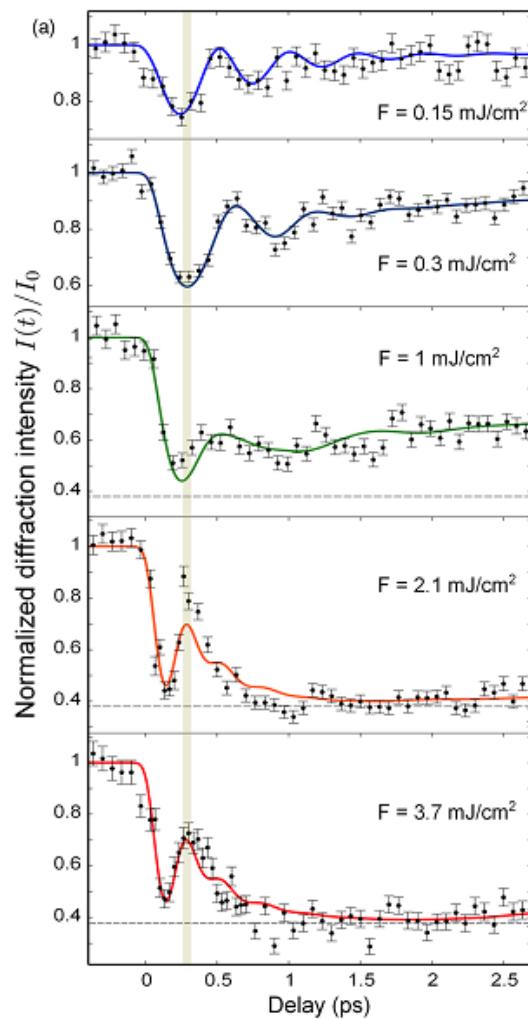
- $F > 1 \text{ mJ/cm}^2$

- No recovery of satellite peak intensity within 10 ps
- Oscillation frequency doubled w/r to the low fluence case

Significant changes of the atomic potential surface

Coherent structural dynamics in blue bronze ($K_{0.3}MoO_3$)

- Time-dependence of the satellite $\left(1 [4 - q_b] \frac{1}{2}\right)$ - Higher fluences



- Free energy vs laser excitation [$\eta \propto$ laser fluence]

$$F = F_0 + \frac{1}{2} \left[\eta e^{-\frac{t}{\tau}} - 1 \right] u_0^2 + \frac{1}{4} u_0^4$$

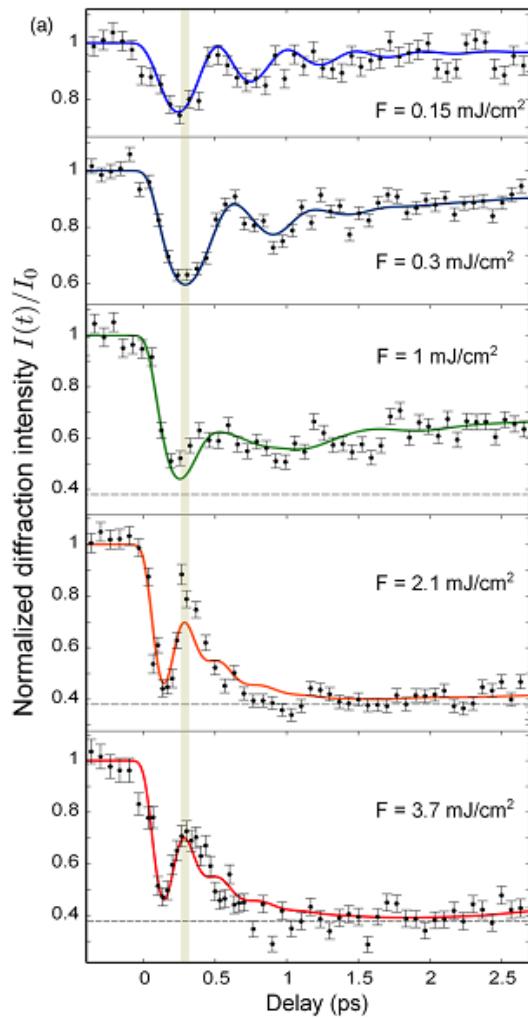
- Equation of motion to be solved:

$$C_1 \frac{\partial^2}{\partial t^2} \left[\frac{u_0(t)}{u_0(t < 0)} \right] = -\overrightarrow{grad} F - C_2 \gamma(t) \frac{\partial}{\partial t} \left[\frac{u_0(t)}{u_0(t < 0)} \right]$$

Non-harmonic motions of atoms

Coherent structural dynamics in blue bronze ($K_{0.3}MoO_3$)

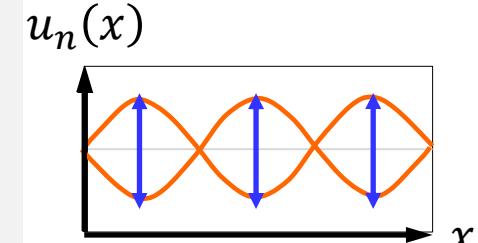
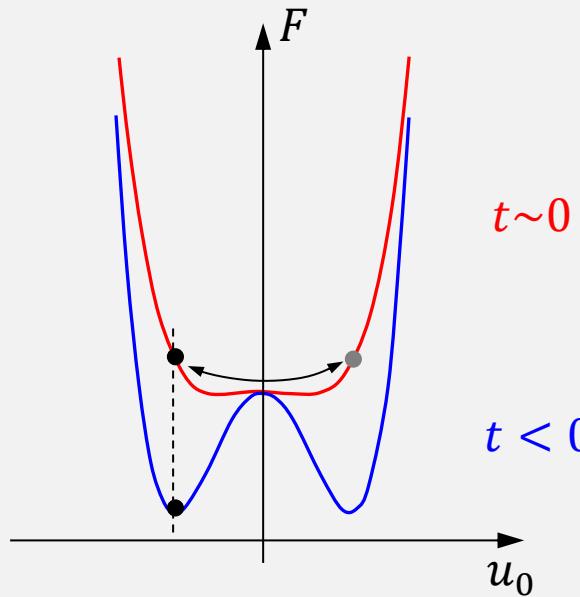
- Time-dependence of the satellite $\left(1 [4 - q_b] \frac{1}{2}\right)$ - Higher fluences



- Origin of the fast oscillations above 1 mJ/cm^2 ?

Free energy

$$F = F_0 + \frac{1}{2} \left[\eta e^{-\frac{t}{\tau}} - 1 \right] u_0^2 + \frac{1}{4} u_0^4$$



Ultrafast change of atomic potential symmetry

Sub-ns and sub-ps structural dynamics: a view from time-resolved X-ray diffraction

I. Scientific motivations

II. Pump-probe diffraction

- Principle
- Time resolution & synchronization
- Short X-ray pulse sources
- Specific geometrical constraints

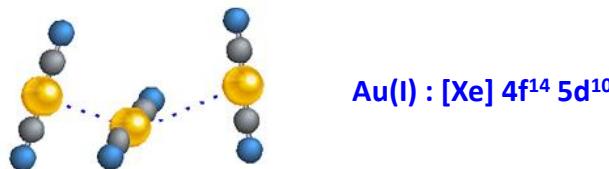
III. Examples

- Photo-induced phase transition in $K_{0.3}MoO_3$
- Ultrafast bond formation in a Gold(I) trimer

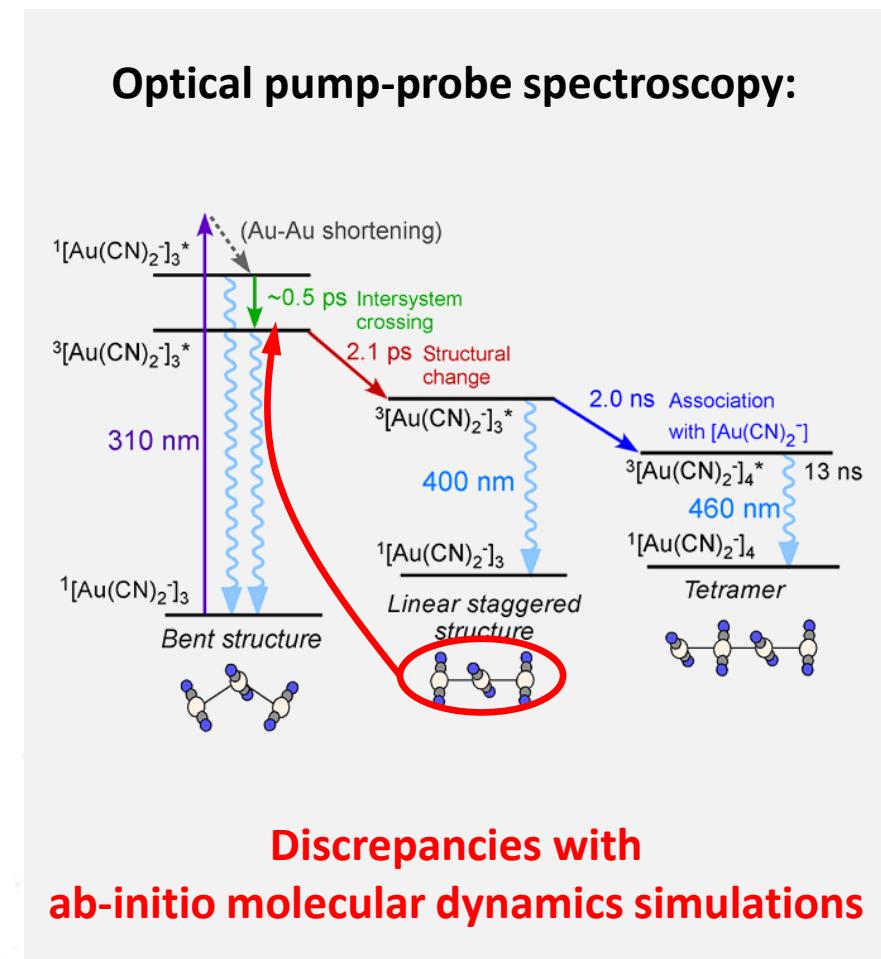
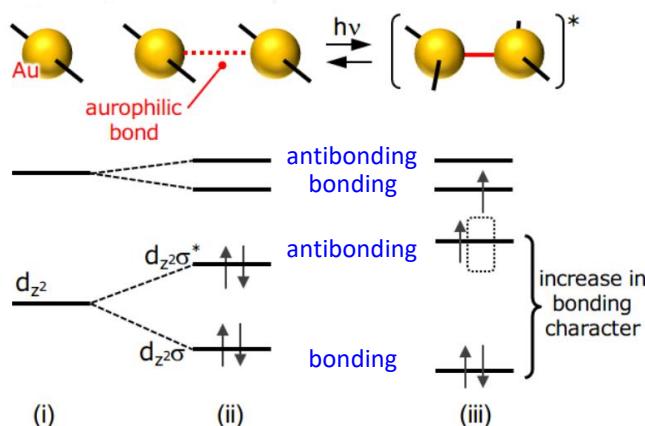


Tight Au-Au bond formation in $[Au(CN)_2^-]$ oligomers

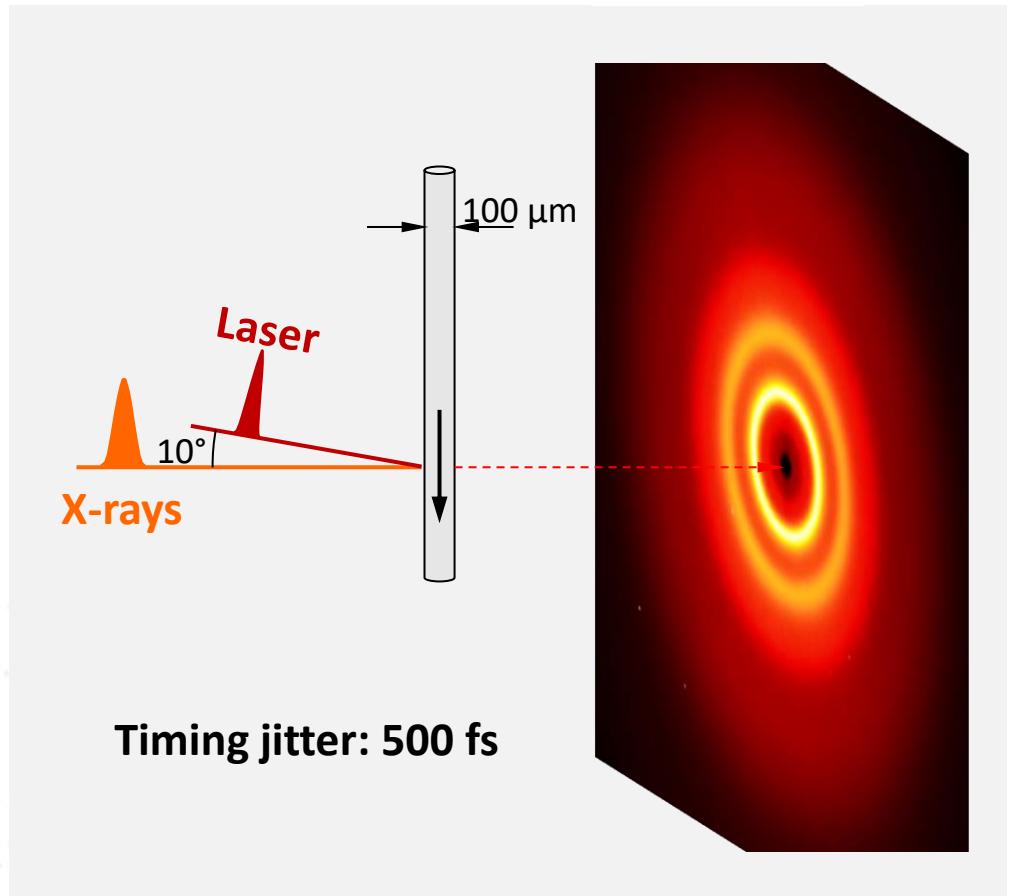
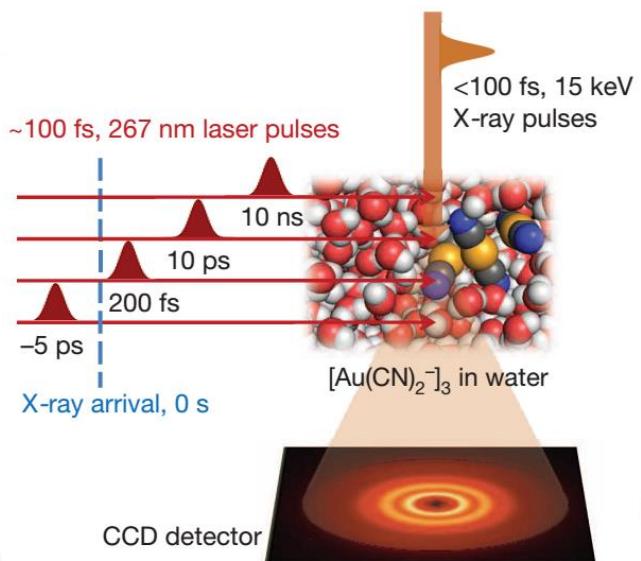
- $[\text{Au}(\text{CN})_2^-]_3$ in aqueous solution



- $[\text{Au}(\text{CN})_2^-]_3$: photoinduced response



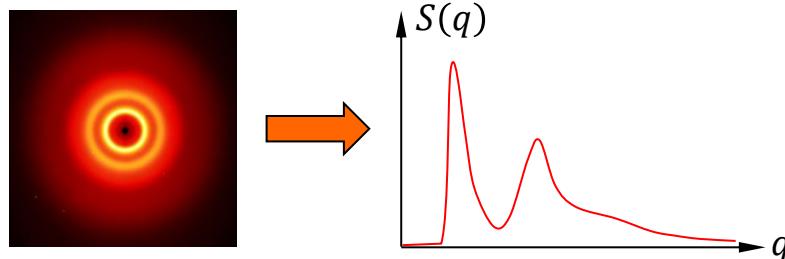
Tight Au-Au bond formation in $[\text{Au}(\text{CN})_2^-]$ oligomers



For each time delay: 50 images taken with 80 X-ray pulses
 $\rightarrow 4 \cdot 10^{15}$ incoming photons

Tight Au-Au bond formation in $[\text{Au}(\text{CN})_2^-]$ oligomers

- Radial integration:



- Scattering function $S(q)$:

$$S(q) = \sum_{\alpha} N_{\alpha} f_{\alpha}^2 + \sum_{\alpha} \sum_{\beta \neq \alpha} \frac{N_{\alpha} N_{\beta}}{V} f_{\alpha} f_{\beta} \int_0^{\infty} [g_{\alpha\beta}(r) - 1] \frac{\sin qr}{qr} 4\pi r^2 dr$$

→ α, β : atomic species

- Partial pair distribution function $g_{\alpha\beta}(r)$:

$$g_{\alpha\beta}(r) = \frac{1}{N c_{\alpha} c_{\beta}} \times \frac{1}{4\pi \rho_0 r^2} \times \sum_{i_{\alpha}} \sum_{i_{\beta} \neq i_{\alpha}} \delta(r - r_{i_{\alpha} i_{\beta}})$$

→ Number of β -type atoms at distance r of an α -type atom



Tight Au-Au bond formation in $[\text{Au}(\text{CN})_2^-]$ oligomers

- $S(q) = S(q)_{\text{solute+cage}} + S(q)_{\text{solvent}}$

$\alpha, \beta = \text{H, O}$
Dominant term !

$\alpha, \beta = \text{Au, C, N, H, O}$

Dominated by Au-Au contributions

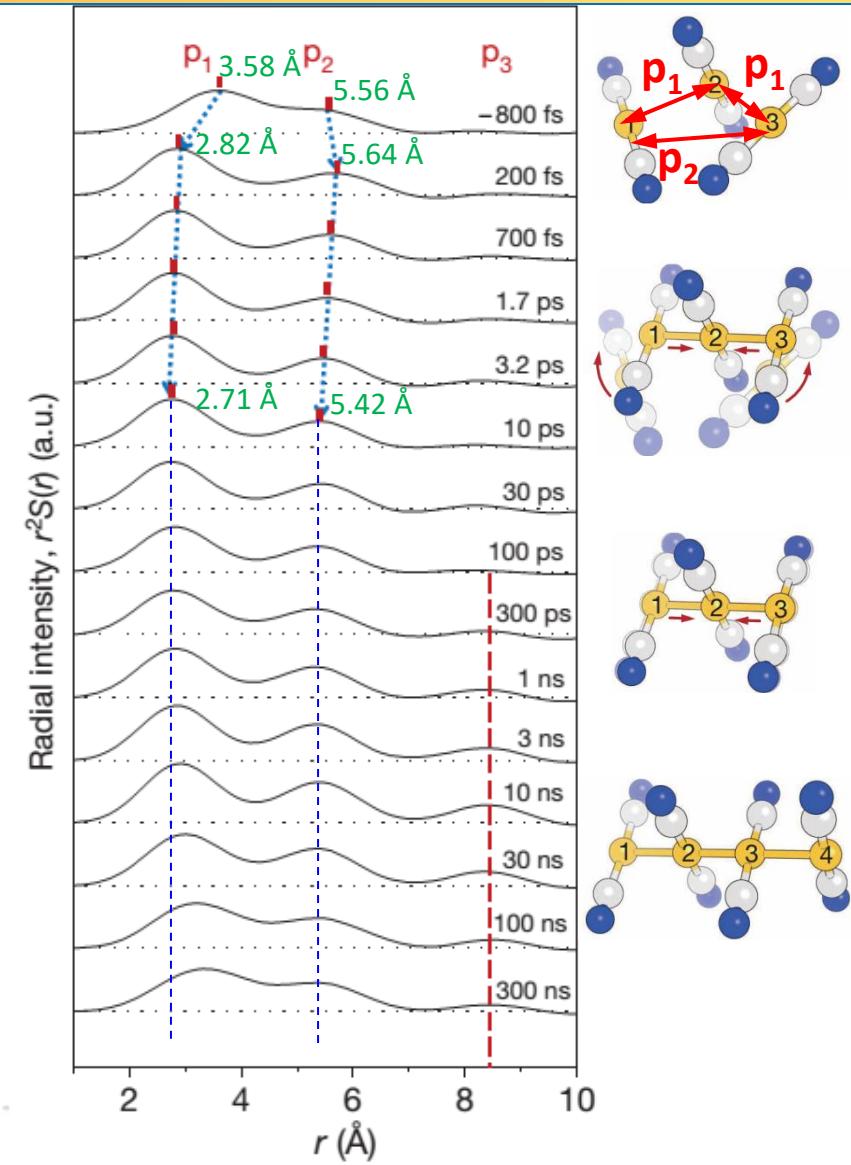
- $\Delta S(q, t) = S(q, t) - S(q, t < 0)$

$$\Delta S(q, t) = \Delta S(q, t)_{\text{Au-Au}} + \boxed{\Delta S(q, t)_{\text{solvent}}}$$

Determined by a separate solvent heating experiment

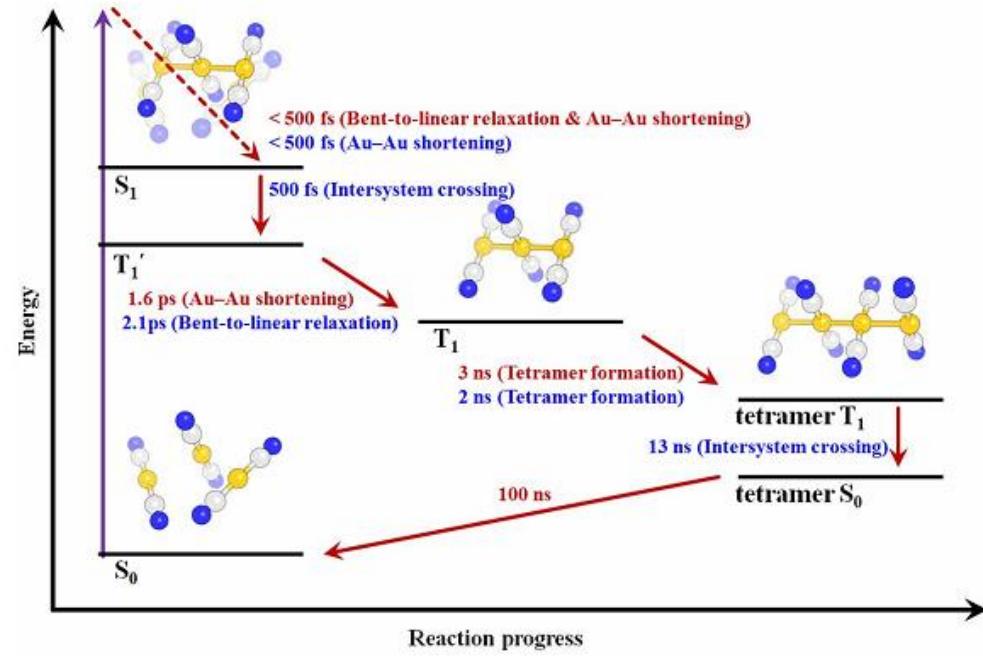
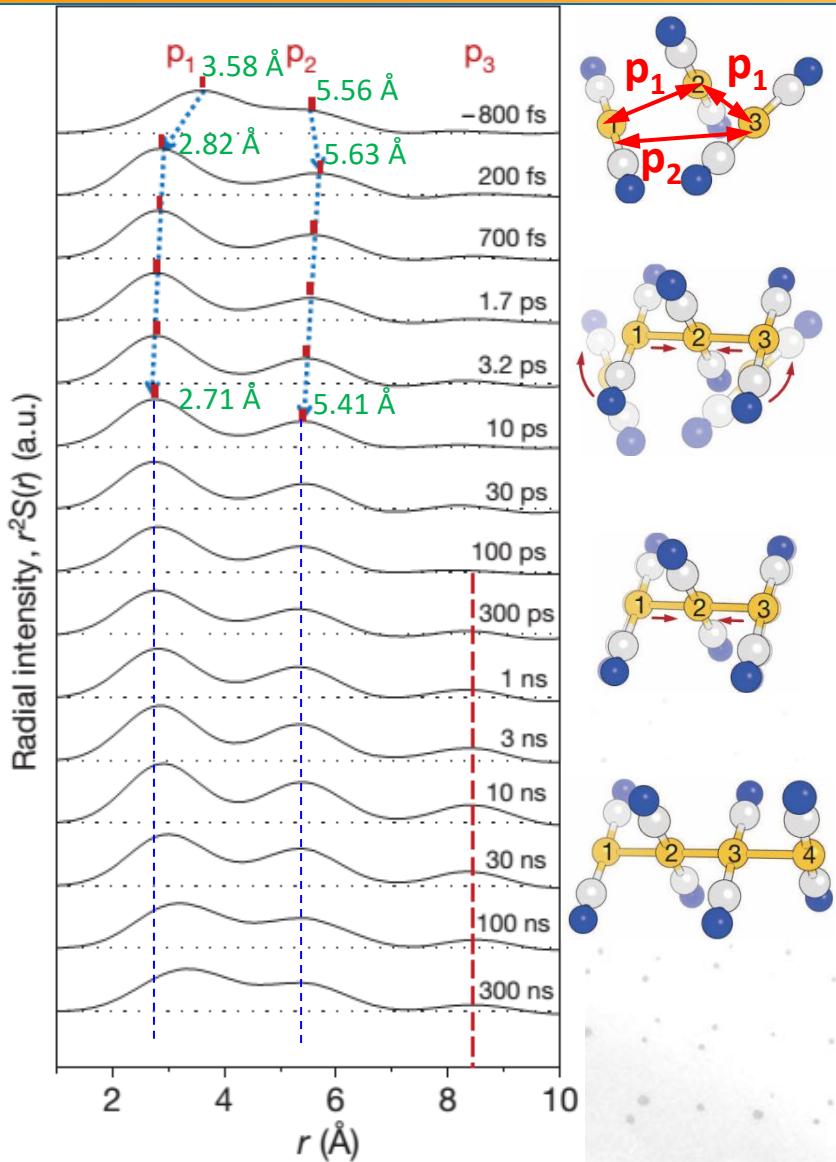
- $\Delta S(q, t)_{\text{Au-Au}} \xrightarrow{\text{FT}} \Delta g_{\text{Au-Au}}(r, t)$

- $g_{\text{Au-Au}}(r, t) = g^0_{\text{Au-Au}}(r) + \Delta g_{\text{Au-Au}}(r, t)$



K.H. Kim *et al.*, Nature 518, 385 (2015)

Tight Au-Au bond formation in $[\text{Au}(\text{CN})_2^-]$ oligomers



Ultrafast change from bent to linear configuration,
within 500 fs

K.H. Kim *et al.*, Nature 518, 385 (2015)

Thank you !

