



# Raman spectroscopy of individual freestanding single-walled carbon nanotubes of defined atomic structure

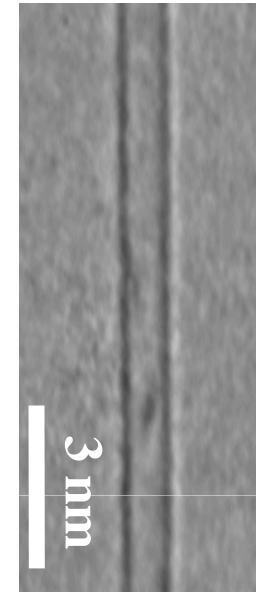
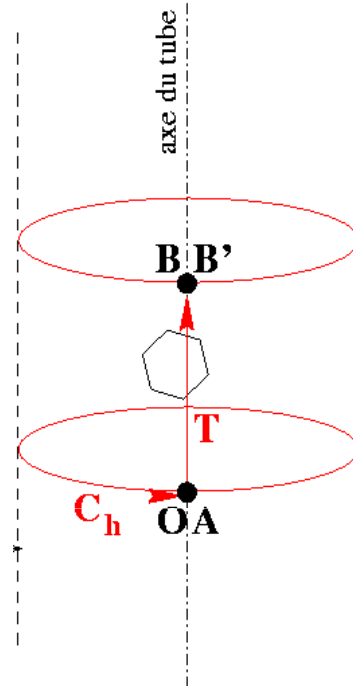
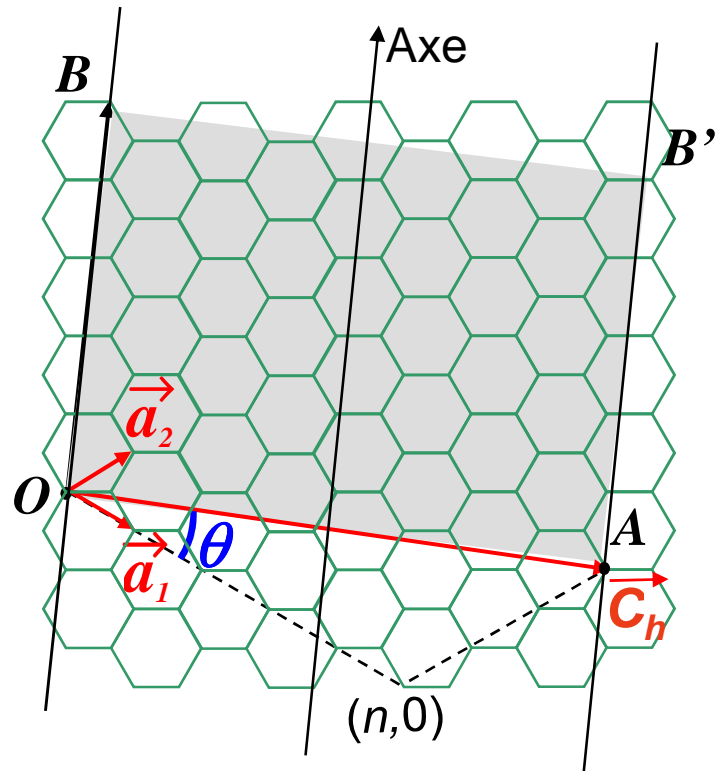
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CNRS - Université Montpellier 2, France



# SWNT structure



$$\vec{C}_h = n\vec{a}_1 + m\vec{a}_2 \longrightarrow \boxed{(n,m)}$$

$$\text{Diameter } d = \frac{|\vec{C}_h|}{\pi}$$

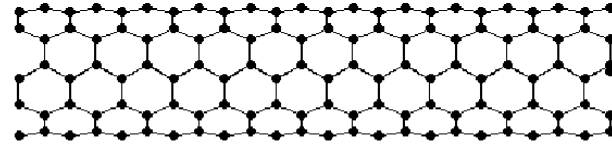
$$\text{Chiral angle } \theta = \text{Arc tan}\left(\frac{m\sqrt{3}}{2n+m}\right)$$

$(n-m) \bmod 3 \Rightarrow \text{Metallic}$

$(n-m) \bmod 3 = 1,2 \Rightarrow \text{Semiconductor}$

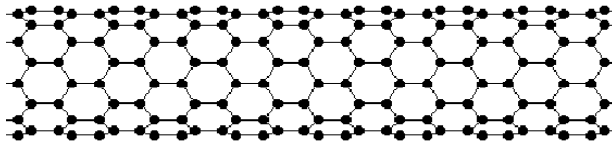
**Tube (n,m)**

n=m *armchair*



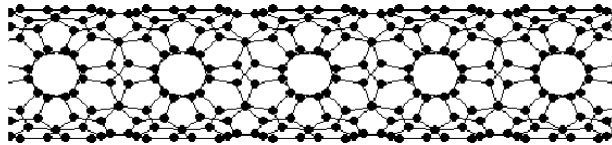
$\theta = 30^\circ$

m=0 *zigzag*



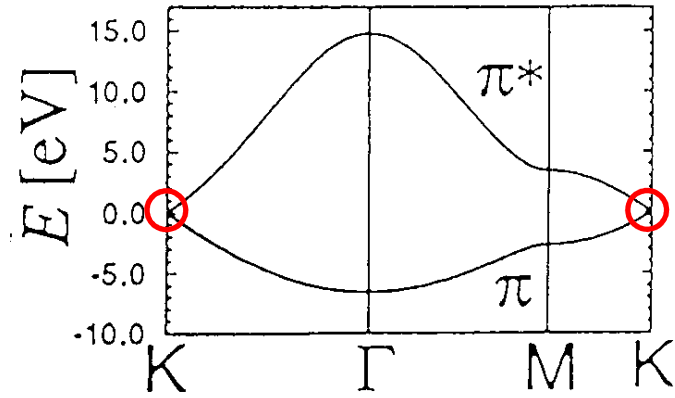
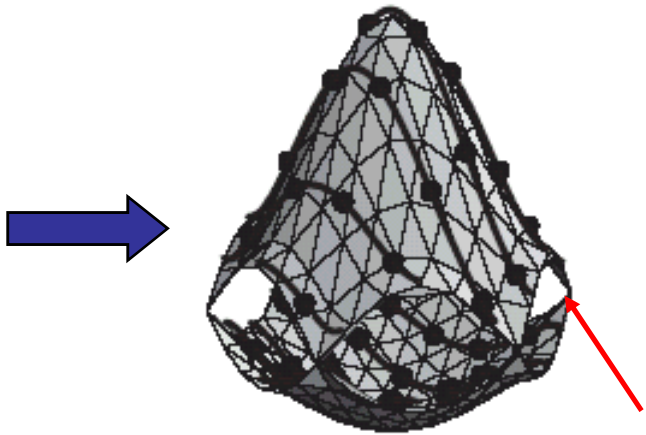
$\theta = 0^\circ$

n,m *chiral*



$0^\circ \leq \theta \leq 30^\circ$

# Electronic properties



**Point K**

$$E_g(\vec{k}) = \pm \gamma_0 \left\{ 3 + 2 \cos(\vec{k} \cdot \vec{a}_1) + 2 \cos(\vec{k} \cdot \vec{a}_2) + 2 \cos[\vec{k} \cdot (\vec{a}_1 - \vec{a}_2)] \right\}^{1/2}$$



$$\vec{K}_{Ch} \vec{C}_h = 2\pi\mu$$

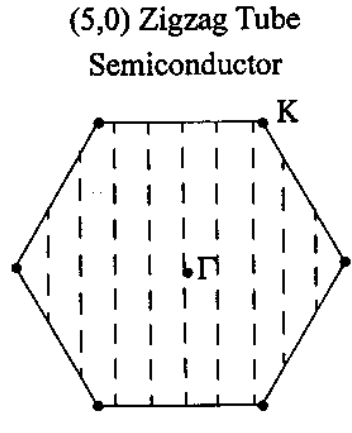
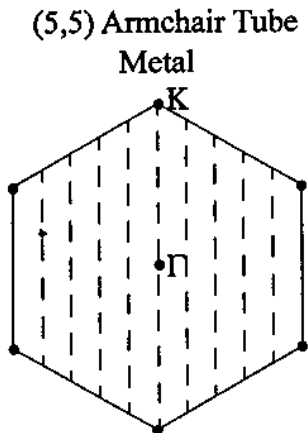
$$\mu = 0, \dots, N-1$$

« Cutting lines »

n-m (2n+m) is a multiple of 3

n-m (2n+m) is not a multiple of 3

↕  
**Metallic**



↕  
**Semiconducting**

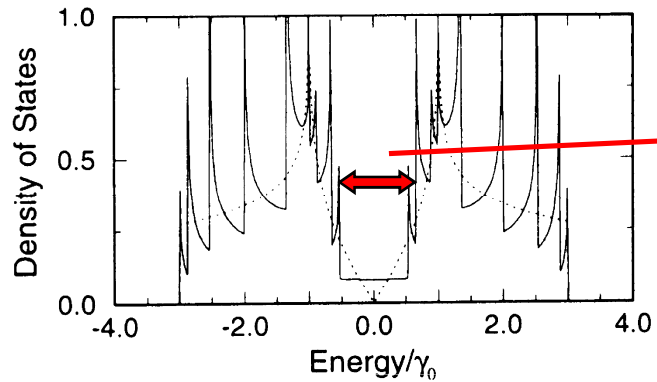
# Optical Transition Energies

$n-m=3p$  Metallic

Kataura plot

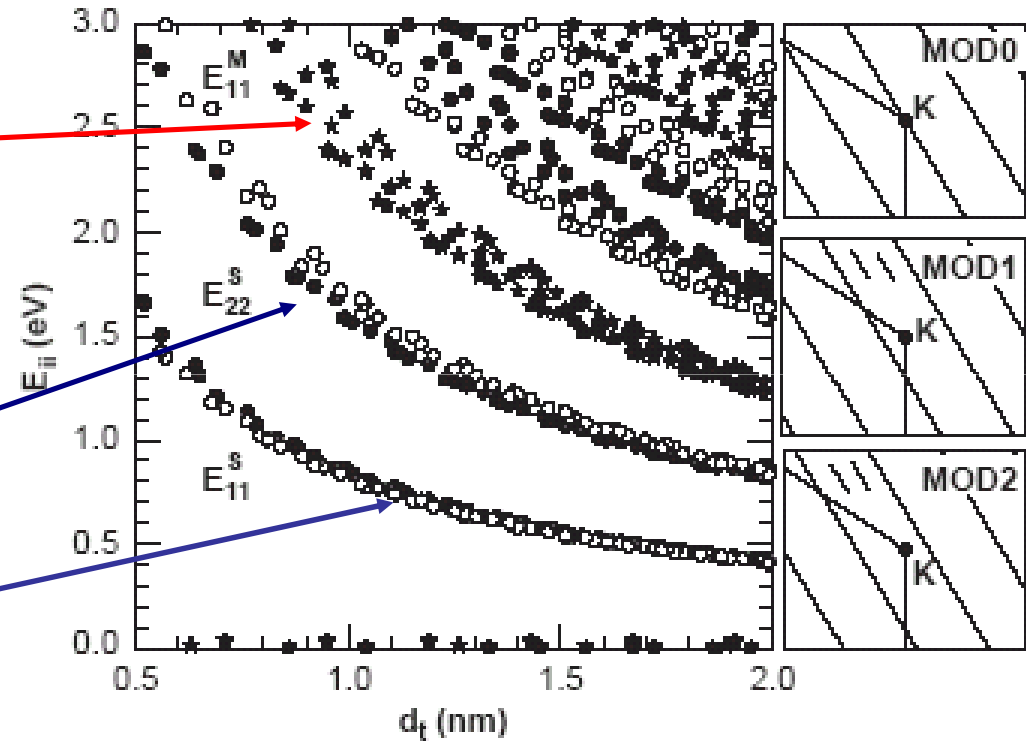
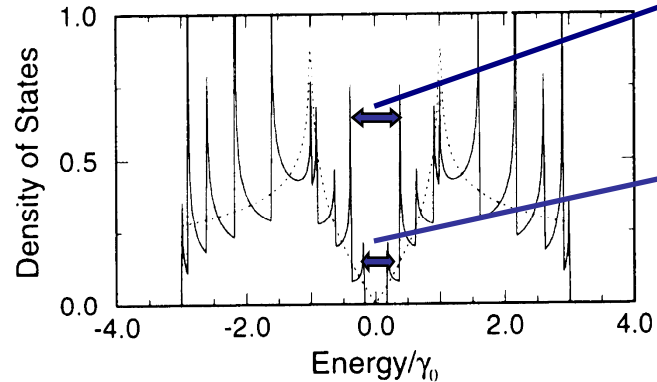
(a)  $(n,m)=(9,0)$

**Metallic**



(b)  $(n,m)=(10,0)$

**Semiconducting**

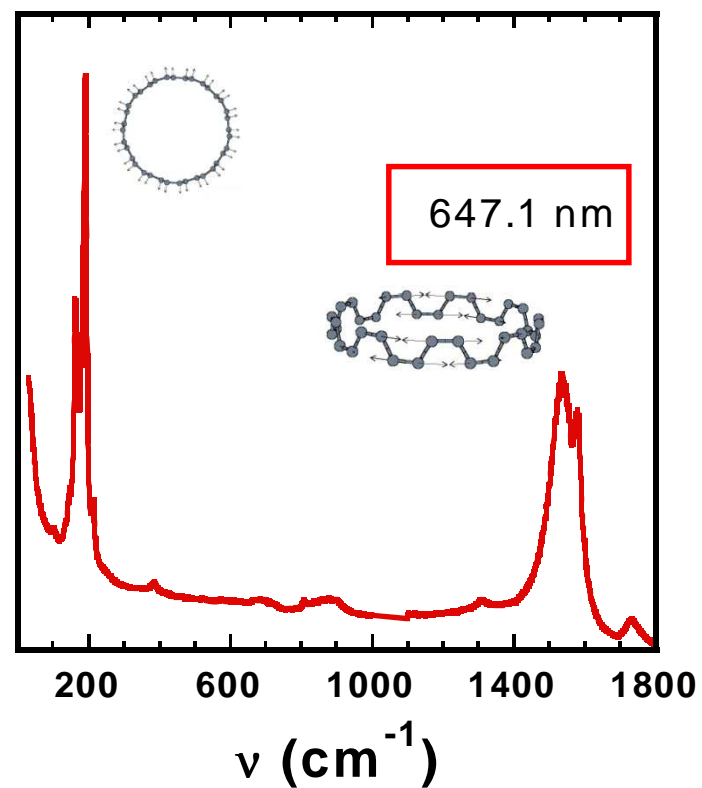
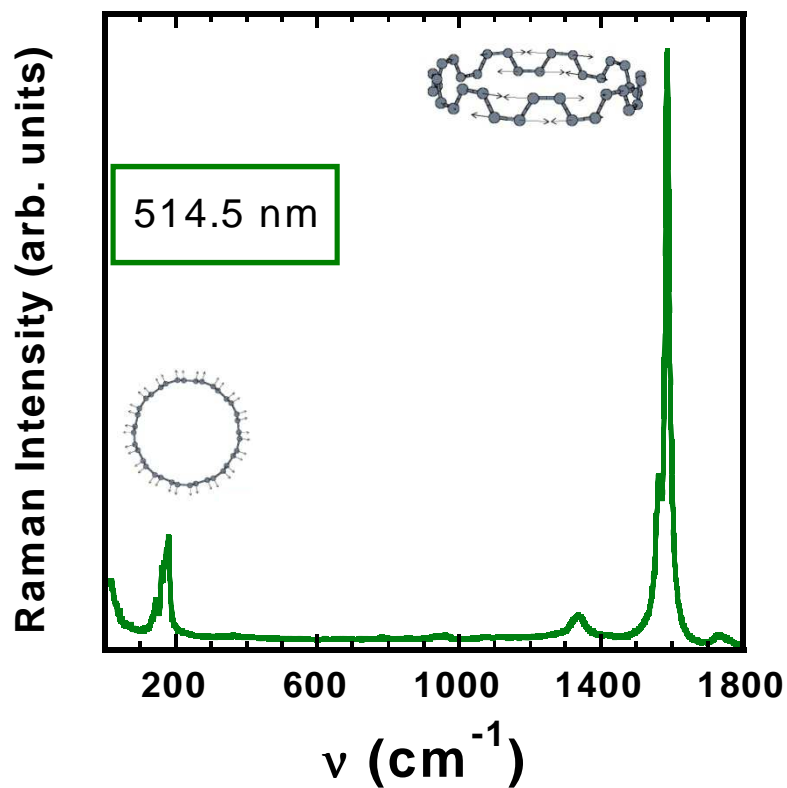
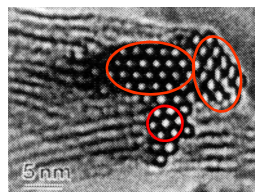
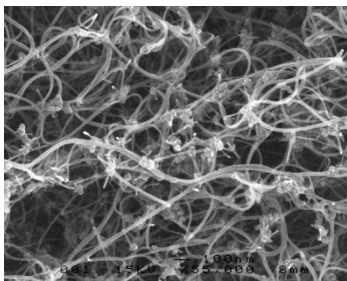


*H. Kataura et al, Synth. Met., 103 (1999) 2555*

*M. Dresselhaus et al, Phys. Reports, 409 (2005) 47*

$n-m \neq 3p$  Semiconducting

# Raman spectroscopy of a nanotube bulk sample



Resonant process

# Lattice structure and Raman spectrum of (n,m) individual, isolated and suspended single-walled carbon nanotubes

## Electron Diffraction and Raman scattering on the same individual SWNT

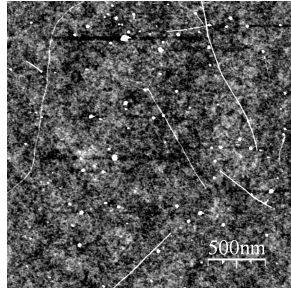
- 1- To prepare individual, isolated and freestanding SWNTs in such a way that access by TEM is possible
- 2- To measure the same SWNT in the electron diffraction and Raman spectroscopy experiments



Perfect localization of the tubes on the samples

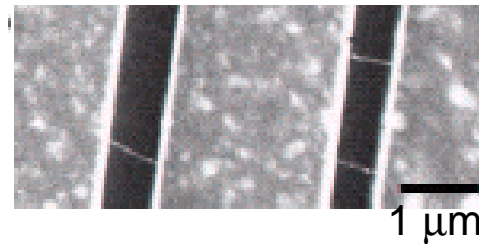
# Experimental Procedure: Samples

## 1- Individual SWNTs suspended between electrodes



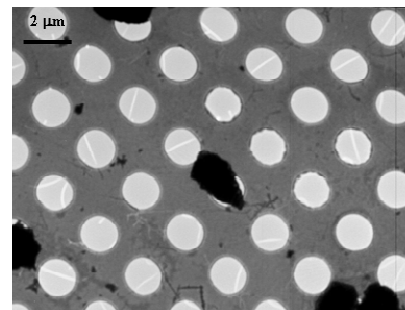
CVD synthesis of SWNTs on Si/SiO<sub>2</sub>  
CH<sub>4</sub> ou C<sub>2</sub>H<sub>4</sub> as carbon feedstocks,  
Low density of nanoparticles of catalyst Ni

E-beam lithography and Etching

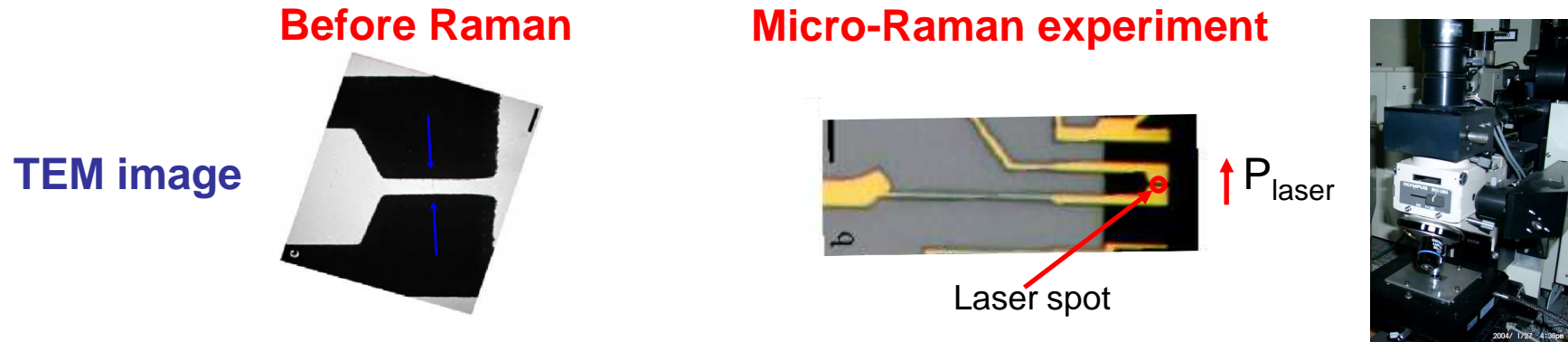


## 2- Individual SWNTs over holes

SiO<sub>x</sub> membranes  
CH<sub>4</sub> as carbon feedstocks



## Experimental procedure



At a fixed excitation energy,  $E_{\text{laser}}$ ,  
we try to detect a **RBM signal** using a **short counting time** (10 s)

If a signal is detected



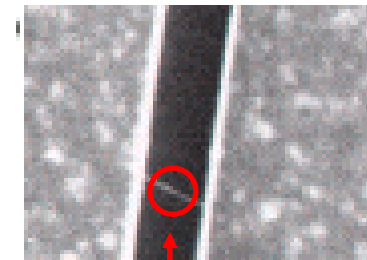
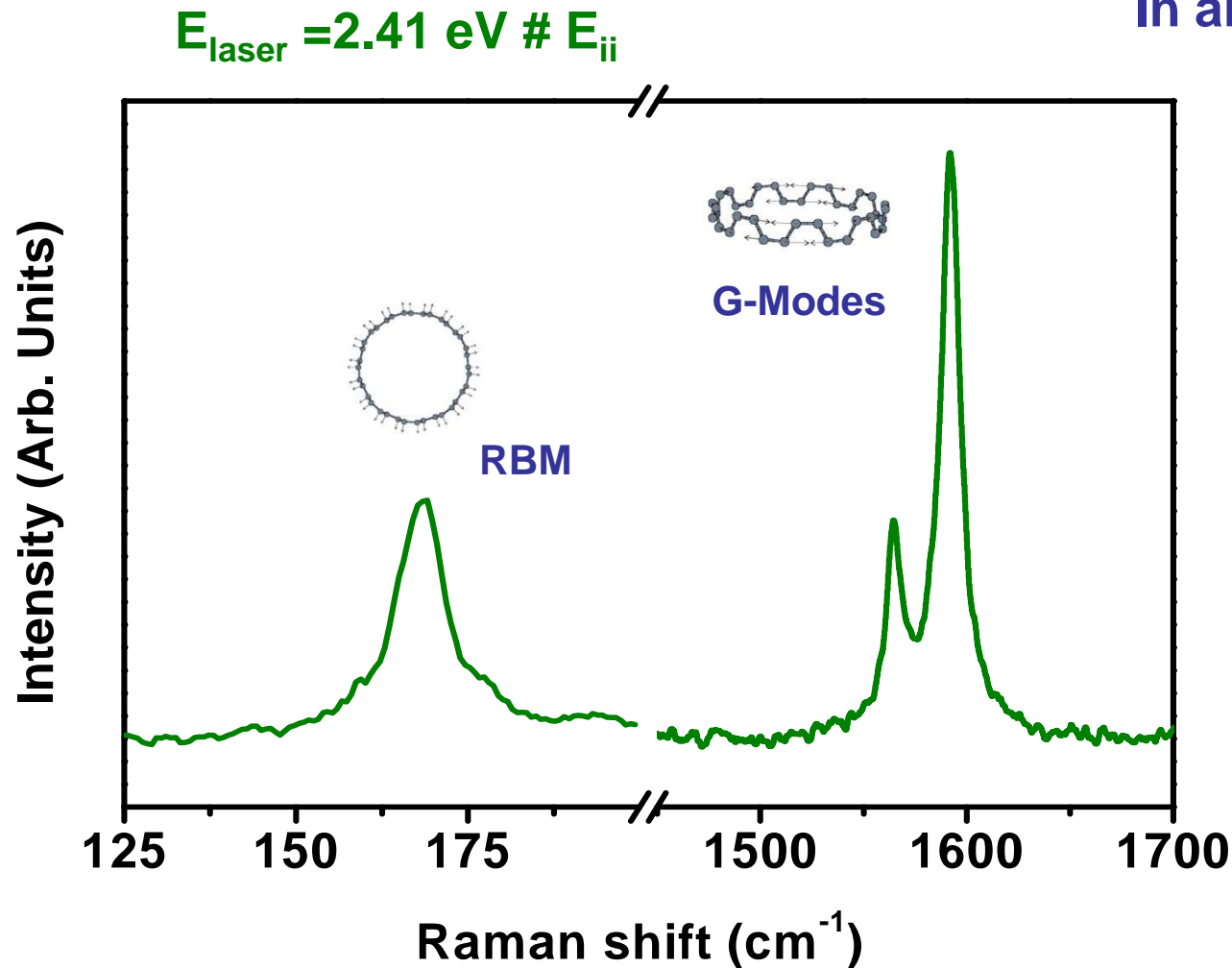
$E_{\text{laser}} \# E_{ij}$



If **no signal is detected**, the excitation energy is changed, and  
we try again to obtain a signal by using a short counting time

# Raman Spectrum of an individual, isolated freestanding SWNT

In air and room temperature



Laser spot

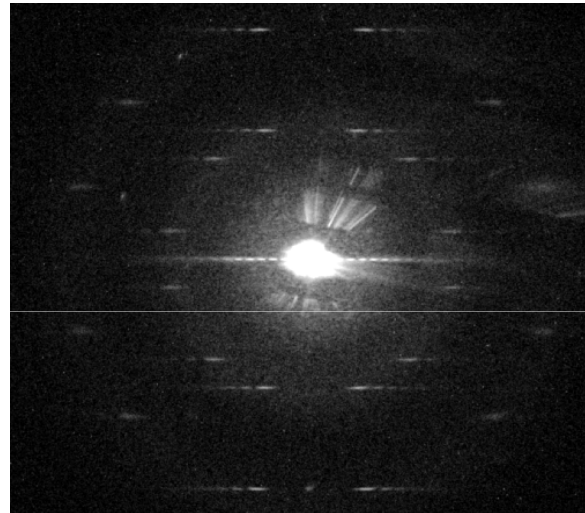
Intrinsic Raman features of the individual SWNT under investigation



**After Raman experiments**, Electron Diffraction experiments were performed on all the nanotubes that showed a Raman signal

J. Meyer  
Max Planck Institut  
Stuttgart

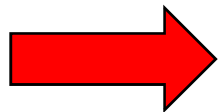
Experiment



Simulation

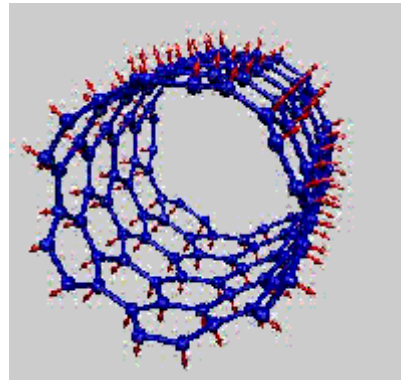


(24,11)



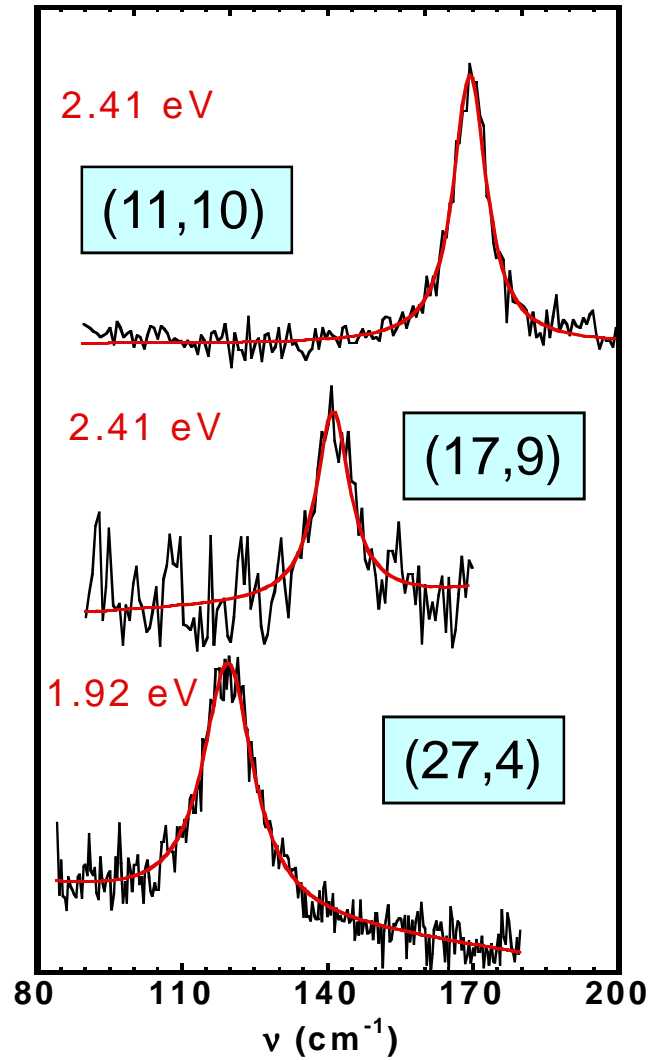
Electron diffraction states if the **Raman spectra** have been measured **on an individual SWNT** or **on a small bundle**

The Radial Breathing Modes  
of  $(n,m)$  individual, isolated and suspended  
single-walled carbon nanotubes

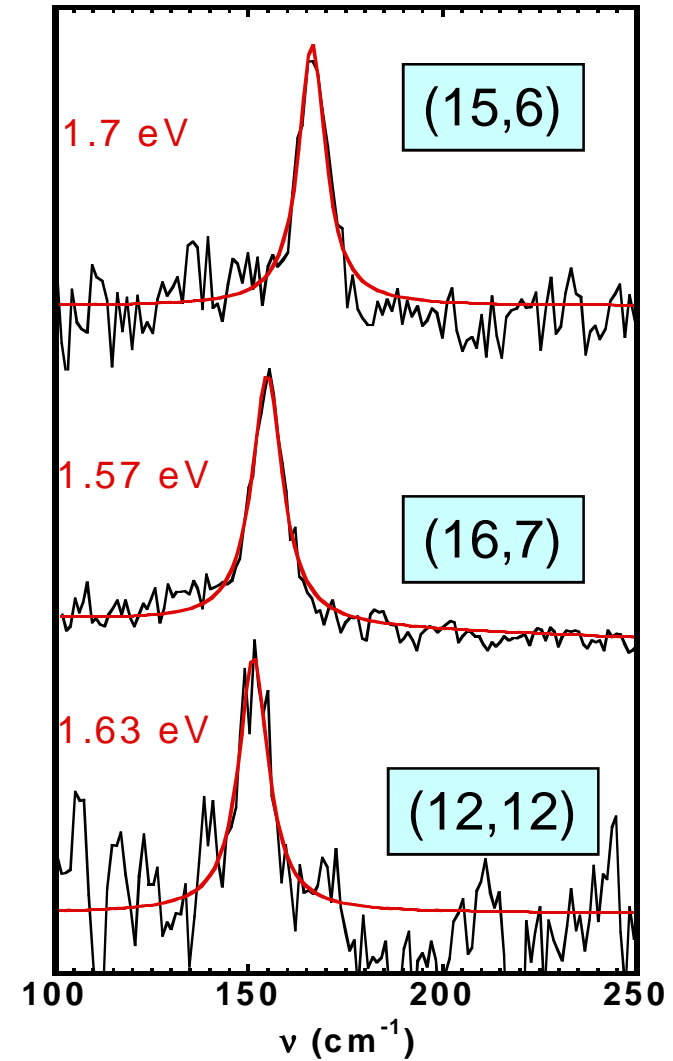


# Radial Breathing Modes

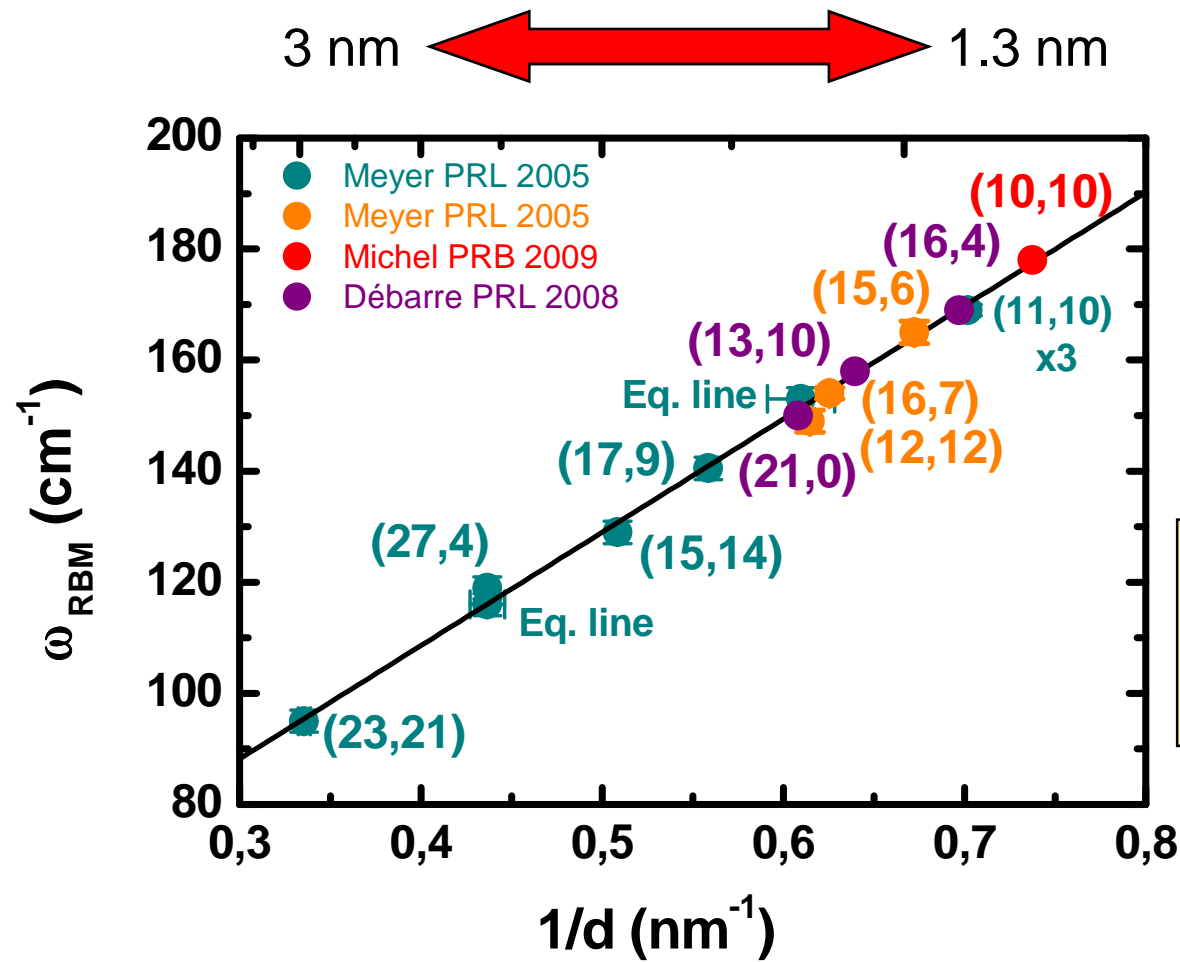
## Semiconducting SWNTs



## Metallic SWNTs



# Radial breathing modes frequency vs diameter



$$\omega_{RBM} (cm^{-1}) = \frac{204}{d(nm)} + 27 cm^{-1}$$

This simple relation allows to derive the diameter of suspended individual nanotube **in air** from the measurement of the RBM frequency

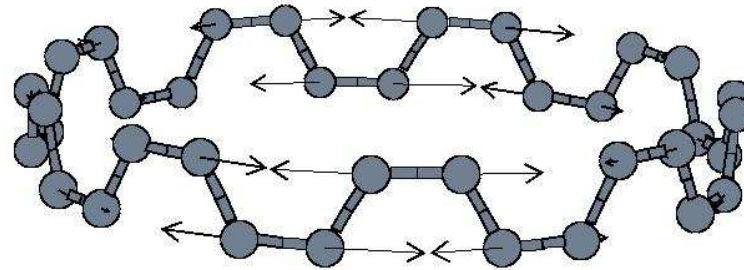
$$\omega_{RBM} (cm^{-1}) = \frac{A}{d(nm)} + B$$

B is associated to environmental effect

**B= 0** with negligible environmental effect

J. C. Meyer *et al.* Phys. Rev. Lett. 95, 217401 (2005)  
 T. Michel *et al.* Phys. Rev. B in press (2009)  
 A. Débarre *et al.* Phys Rev. Lett. 101, 197403 (2008)

# The G-modes of (n,m)-well identified SWNTs



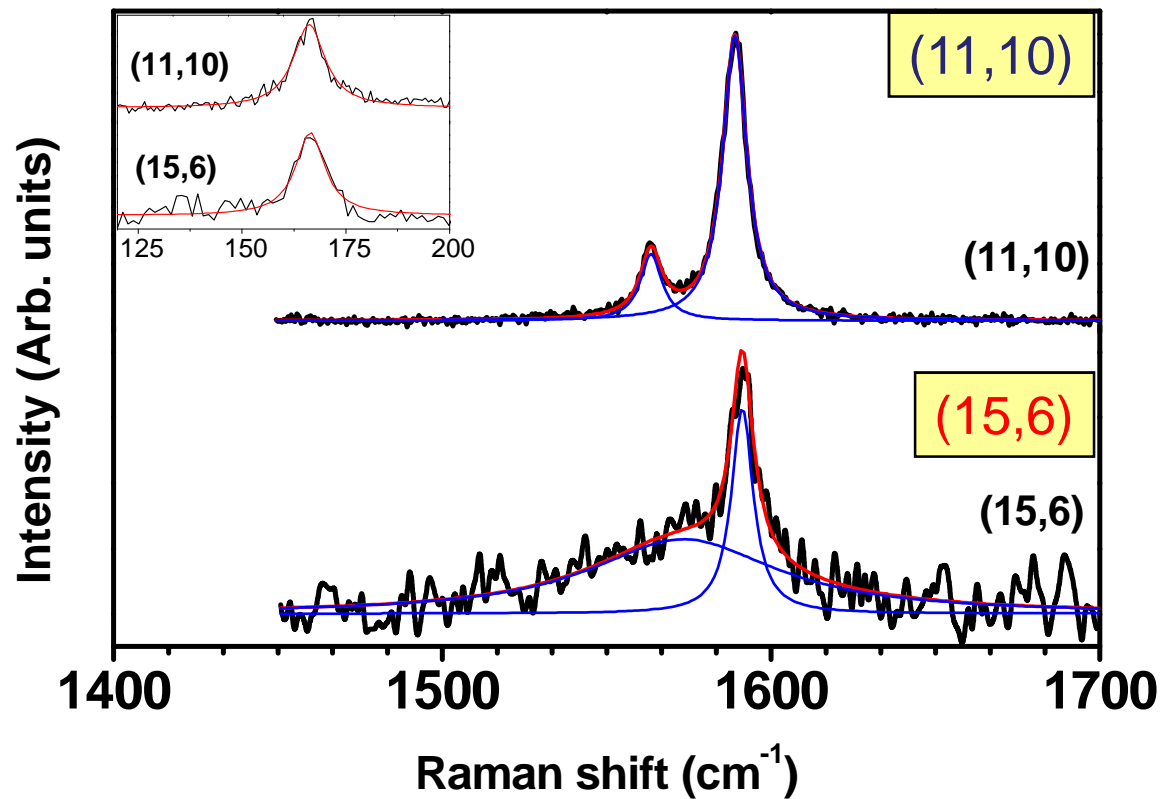
# G-modes of Chiral SWNTs

// // Polarization  
Chiral SWNTs



2 A<sub>1</sub> G-modes  
as expected by calculations

Close diameters  $\approx 1.45$  nm



**Semiconducting**

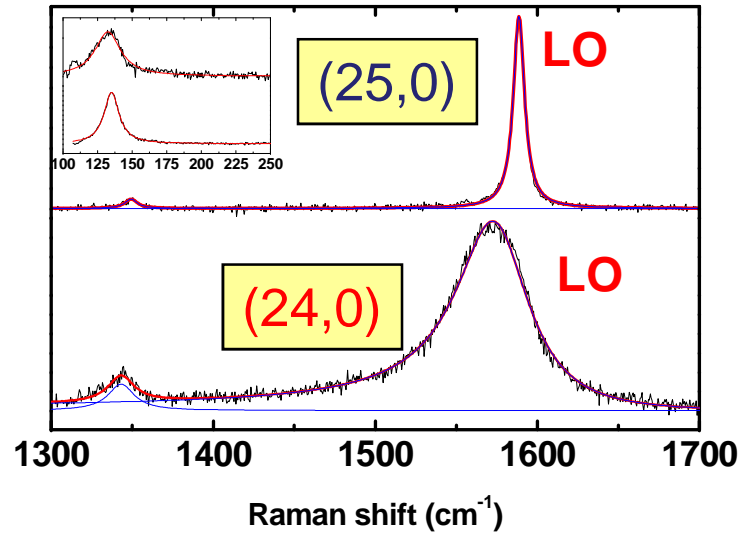
2 narrow peaks

**Metallic**

1 narrow and 1 broad peak

# G-modes of Achiral SWNTs

## ZigZag ( $m = 0$ )



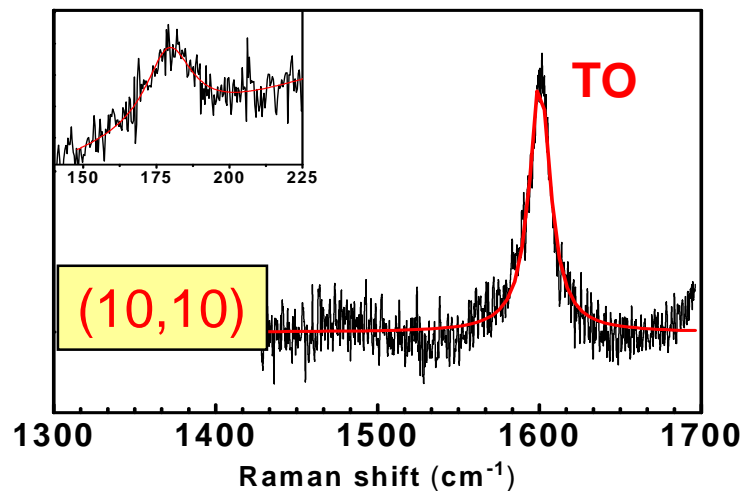
**Semiconducting**

**1 narrow peak**

**Metallic**

**1 broad peak**

## Armchair ( $n = m$ )



**Metallic**

**1 narrow peak**

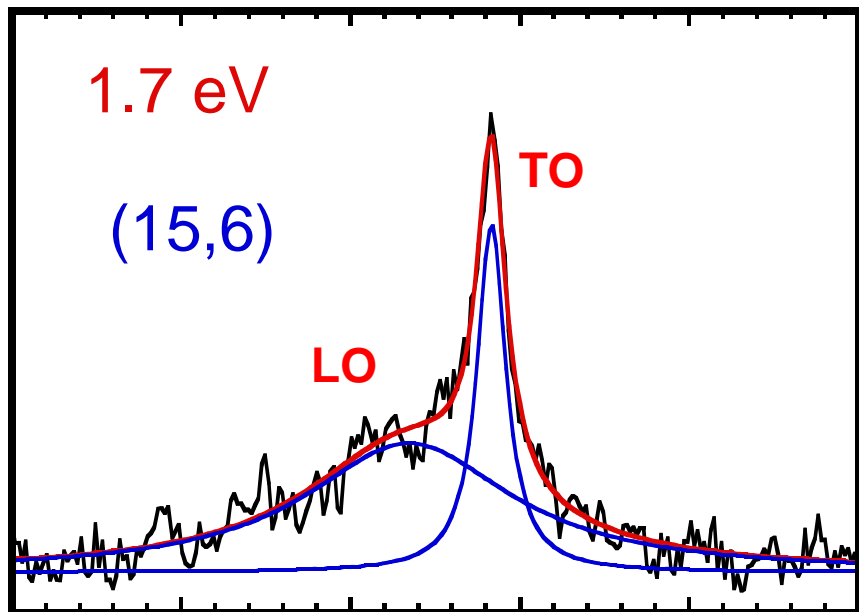
T. Michel *et al.* Phys. Rev. B in press (2009)

# G-modes of **Metallic** SWNTs

(15,6) SWNT

Diameter = 1.47 nm

In resonance with the  $E_{11}^M$  transition

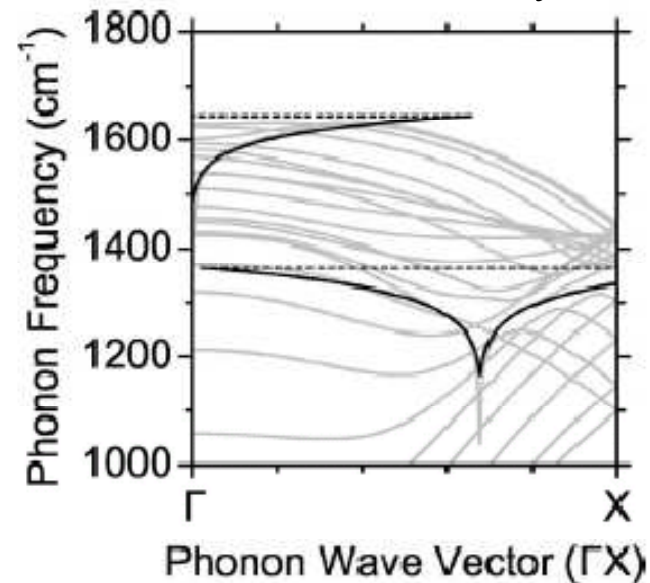


1450 1500 1550 1600 1650 1700  
Raman shift ( $\text{cm}^{-1}$ )

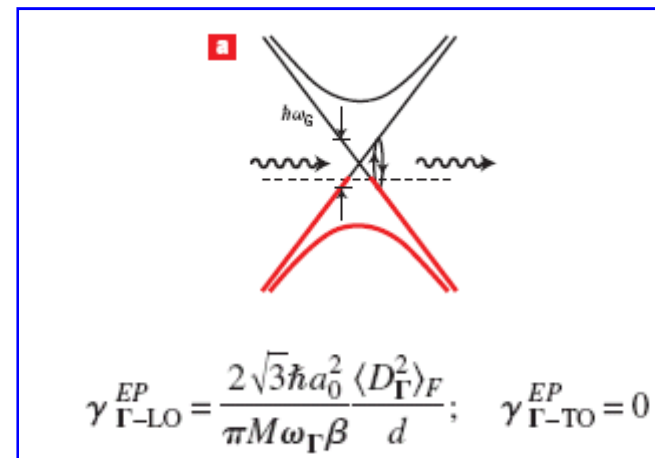
$$I(\omega) = I_1 \frac{[1 + 2(\omega - \omega_1)/q\Gamma_1]^2}{1 + [2(\omega - \omega_1)/\Gamma_1]^2} + I_2 \frac{1}{1 + [2(\omega - \omega_2)/\Gamma_2]^2}$$

Breit-Wigner-Fano (BWF)

Kohn anomaly

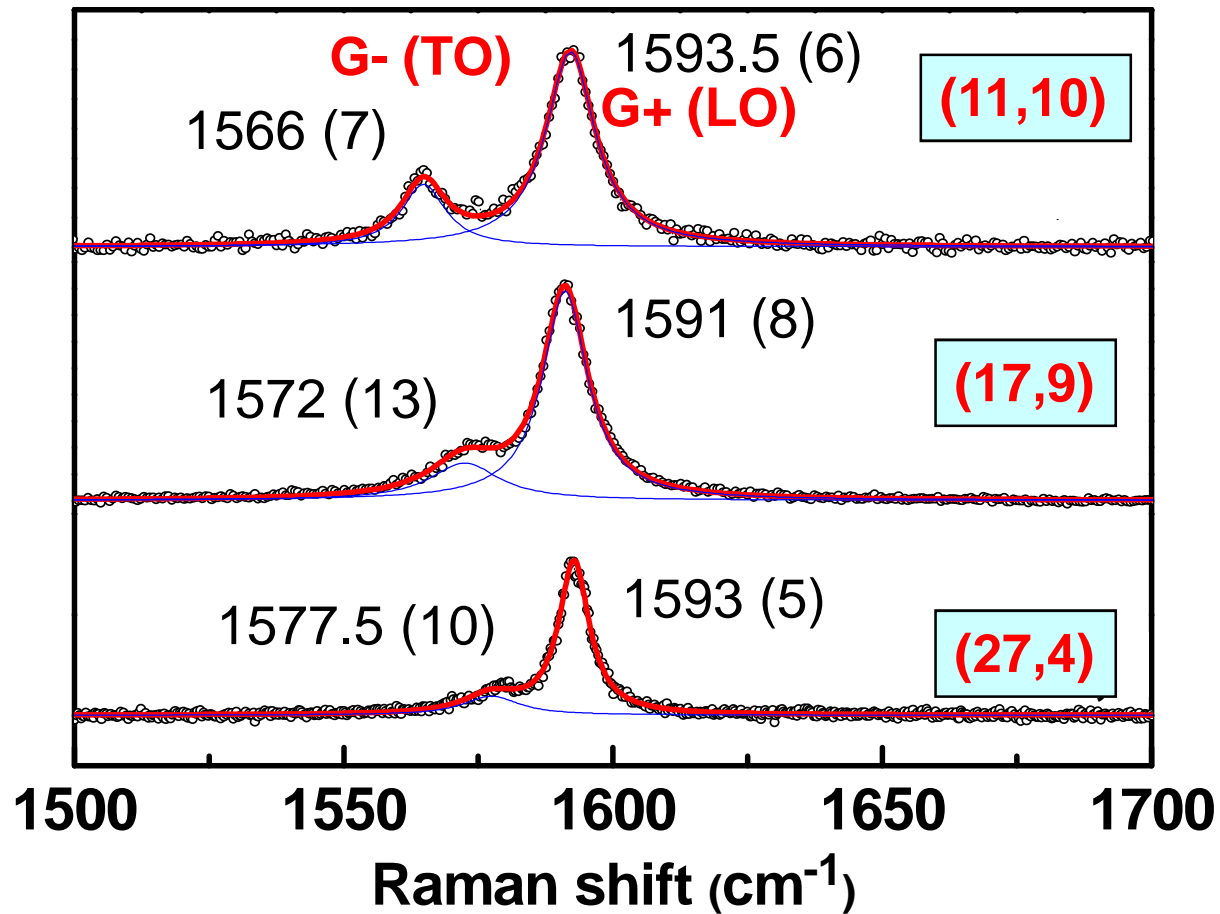


*G.G. Samsonidze et al, PRB 75 (2007) 155420*



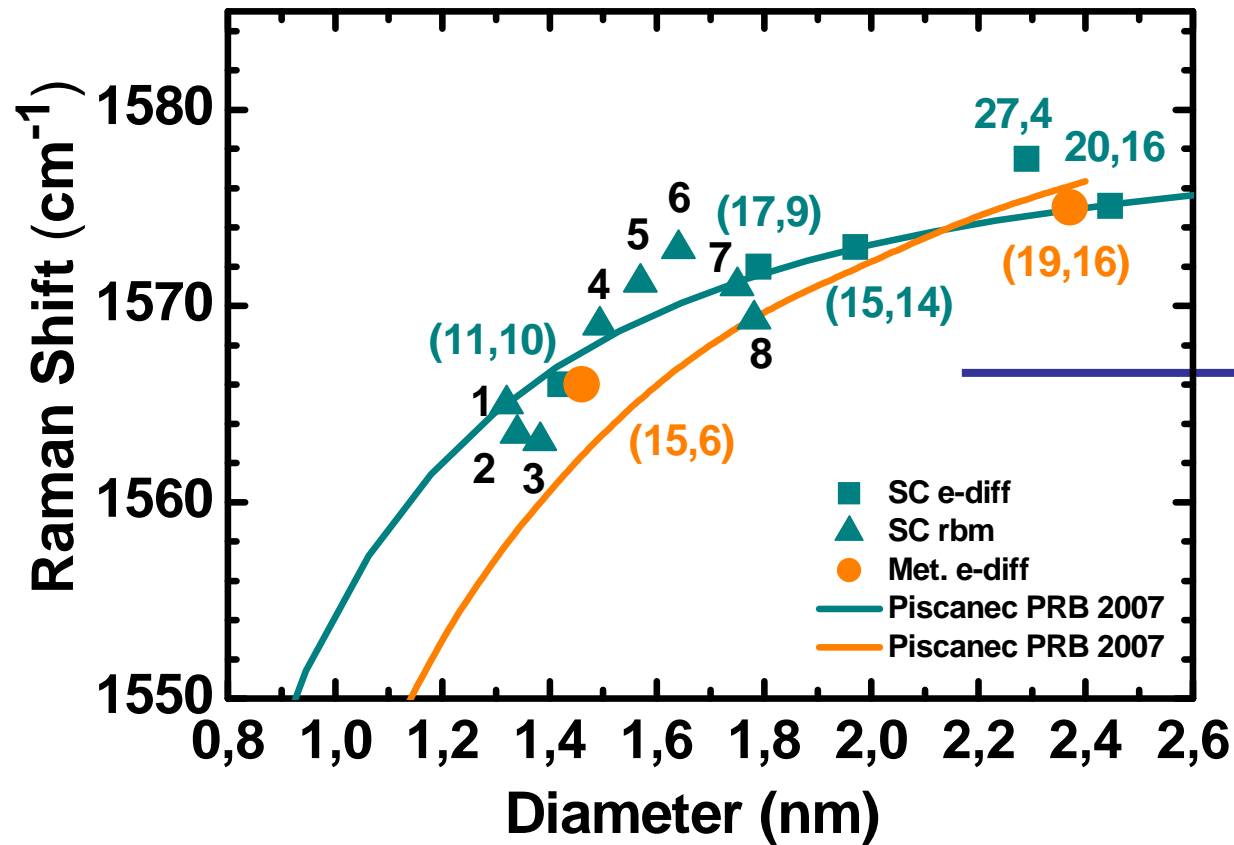
*M. Lazzeri et al., PRB 73 (2006) 155426*

## G-modes of Semiconducting SWNTs



**G- frequency varies with diameter**  
**G+/G- intensity ratio depend on both diameter and chiral angle**

## Frequencies of G- modes



**A tool to determine the diameter of a nanotube under investigation**

Achiral nanotubes : 1 G mode ( $A_{1g}$ )  
 // // Polarization  
 Chiral nanotubes : 2 G modes ( $A_1'$ )

# Optical Transition Energies

At a fixed excitation energy,  $E_{\text{laser}}$ ,  
If a **RBM signal** is detected by using a **short counting time**

$$E_{\text{laser}} \# E_{\text{ii}}$$

# Energy Transitions of individual SWNTs

## Experimental transitions energies

$E_{\text{laser}} \# E_{\text{ii}}$

Semiconducting

(11,10)	2.41 eV
(17,9)	2.41 eV
(15,14)	1.92 eV
(27,4)	1.92 eV
(23,21)	1.60 eV

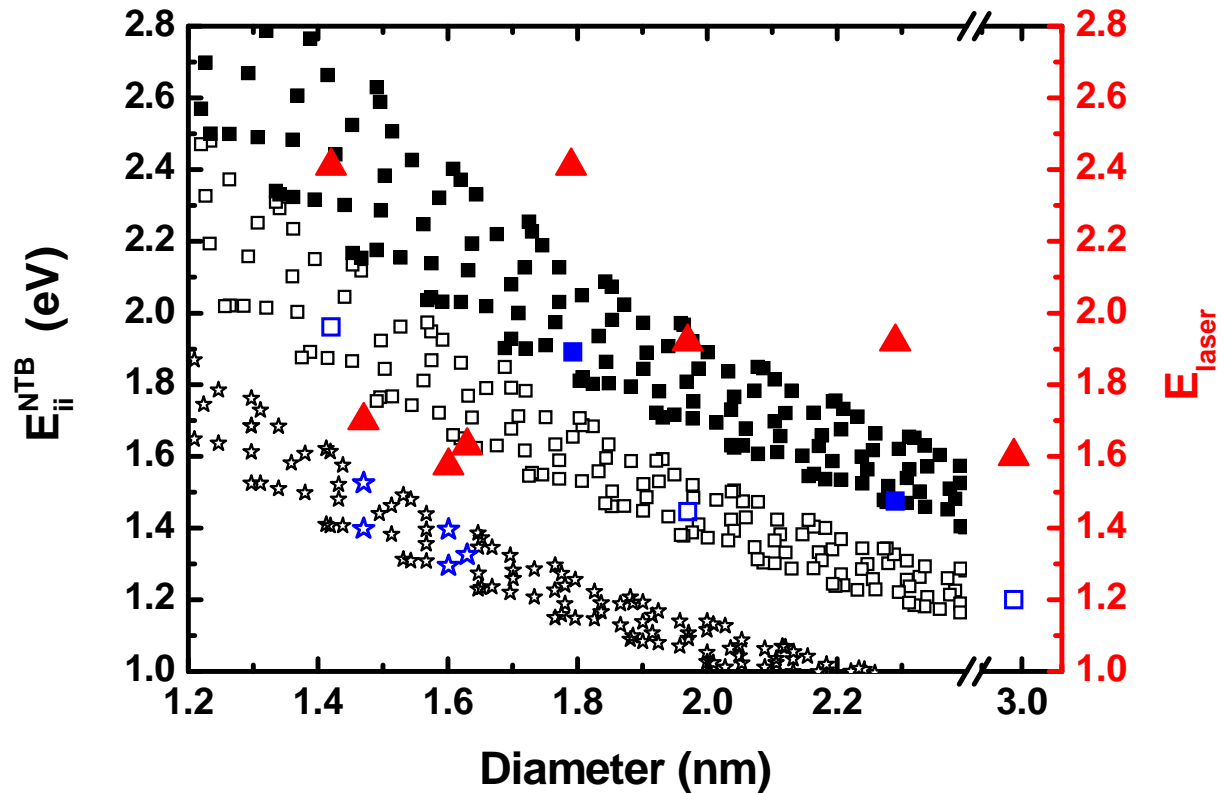
Metallic

(15,6)	1.70 eV
(16,7)	1.57 eV
(12,12)	1.64 eV

M. Paillet *et al.*, PRL **96** (2006) 257401  
 T. Michel *et al.*, PRB **75** (2007) 155432  
 T. Michel *et al.*, Phys. Rev. B in press (2009)

## Calculated transition energies

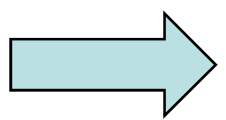
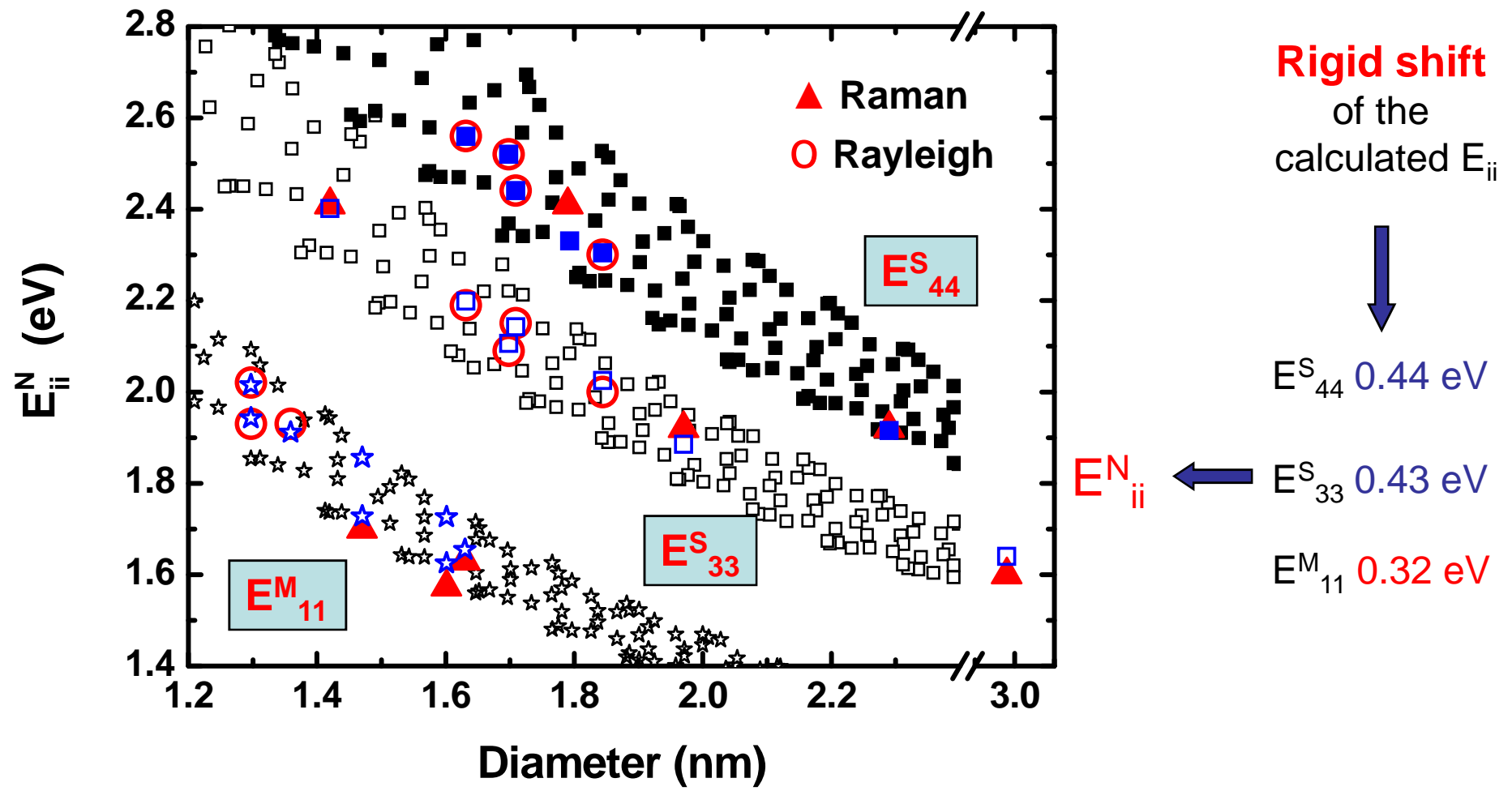
V. N. Popov, New J. Phys. **6** (2004) 1-17  
 V. N. Popov and L. Henrard, PRB **70** (2004) 115407



M. Paillet et al., PRL **96** (2006) 257401

Combined Raman-Electron diffraction: T. Michel et al., PRB **75** (2007) 155432  $\rightarrow$   $\blacktriangle$

Combined Rayleigh –Electron diffraction: M. Y. Sfeir et al., Science **312** (2006) 554  $\rightarrow$   $\circ$



The best estimation of the  $E_{11}^M$ ,  $E_{33}^S$  and  $E_{44}^S$  optical transitions for individual nanotubes in the 1.2-3 nm diameter range

# Identification of SWNT from Raman scattering

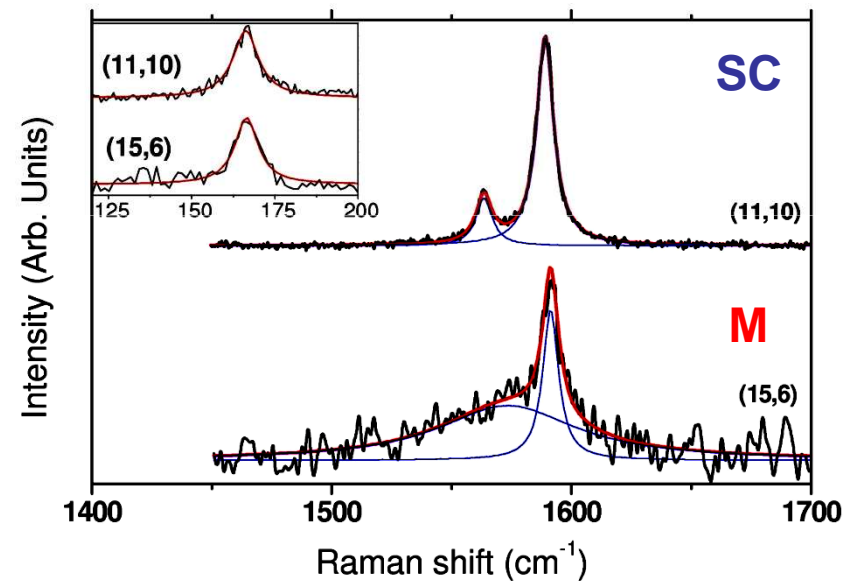
# Raman criteria for the identification of SWNTs

RBM frequency  $\longrightarrow$  Diameter,  $d$

Line shape of the G-modes  $\longrightarrow$  Chiral angle, M or SC character

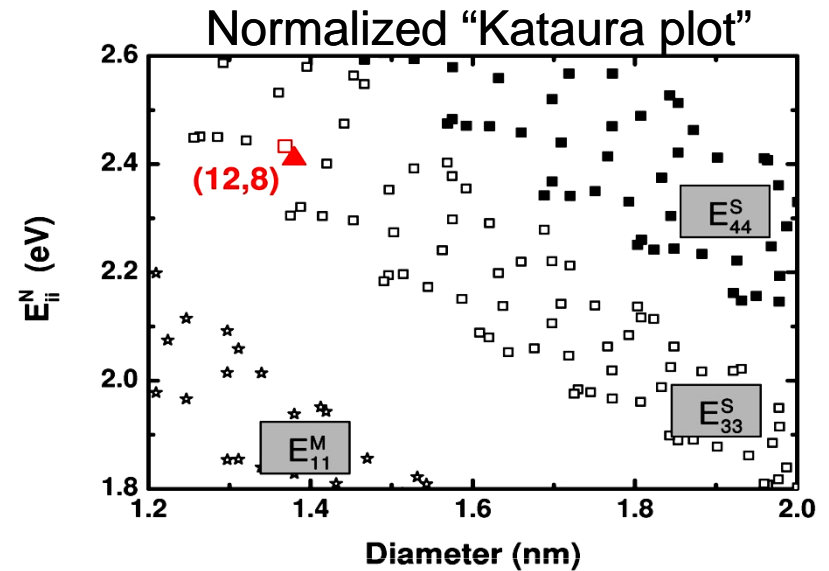
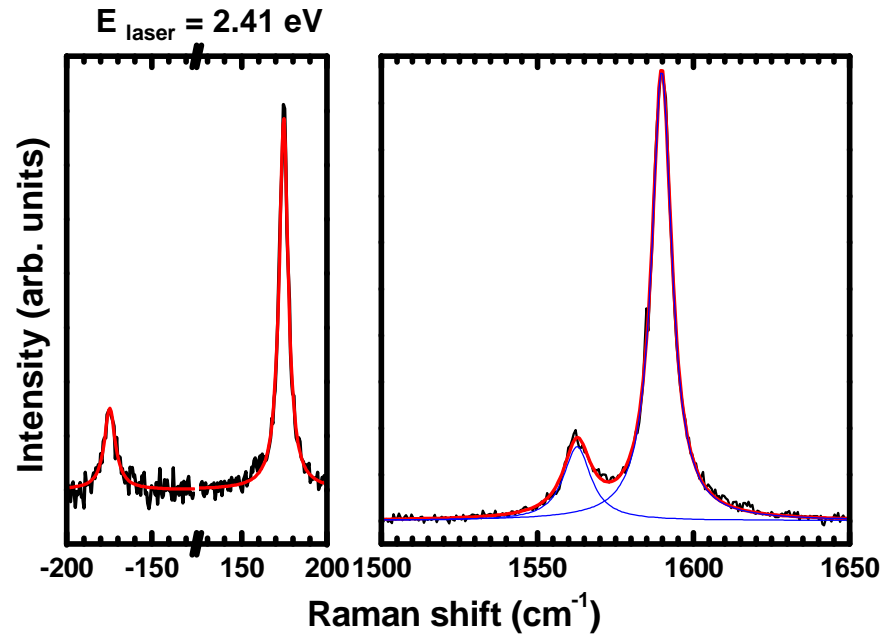
G- frequency  $\longrightarrow$  Diameter,  $d$

Resonance energy  $\longrightarrow$   $E_{ij}$



$(d, E_{\text{laser}})$  in normalized Kataura plot  $\longrightarrow$   $(n, m)$  if the tube is individual

# Identification of an individual SWNT



RBM @  $174.6 \text{ cm}^{-1}$   $\rightarrow$   $d = 1.38 \text{ nm}$

G-mode profile  $\rightarrow$  semiconducting

TO @  $1563 \text{ cm}^{-1}$   $\rightarrow$   $d \approx 1.4 \text{ nm}$

High signal @  $2.41 \text{ eV}$   $\rightarrow$   $E_{33} \approx 2.41 \text{ eV}$

$\rightarrow$  **(12,8)**  $d = 1.37 \text{ nm}$   
 $E_{33} = 2.43 \text{ eV}$

# Conclusions

Raman Spectroscopy / Electronic Diffraction

**Structure / Properties**

Criteria for nanotube identification by Raman only  
have been defined

**Metrologic Approach**

*In-situ* identification of nanotubes

During measurements of photoluminescence,  
transport, phototransport,...